



International
Centre for
Radio
Astronomy
Research



The Power of Simultaneous Multi-Frequency Observations for mm-VLBI and Astrometry

Maria J. Rioja

in collaboration with:

Richard Dodson (ICRAR,Au)

Jose Luis Gomez, Sol Molina (IAA,Sp)

Taehyun Jung, Bong Won Sohn (KASI, Kr)



Curtin University



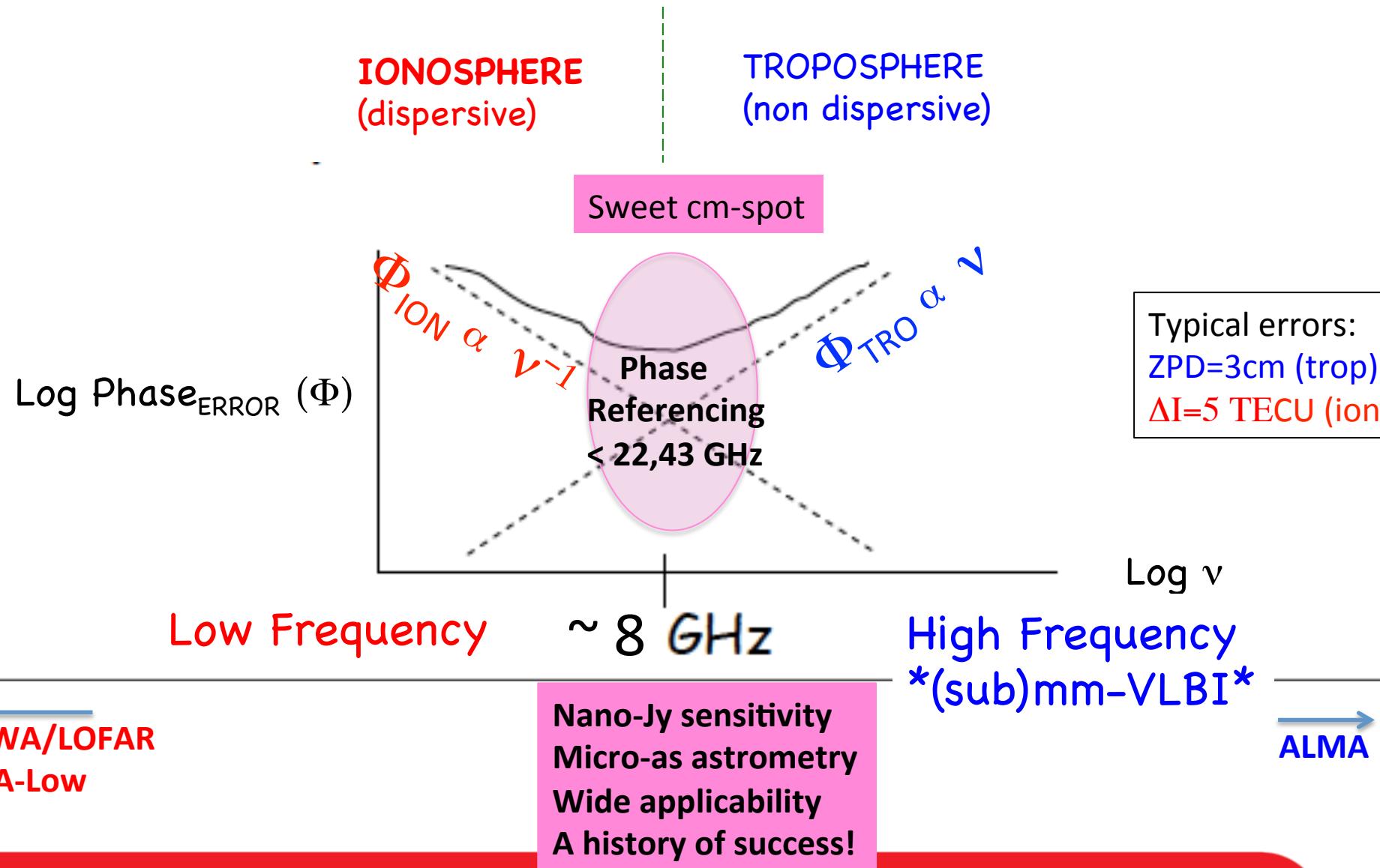
THE UNIVERSITY OF
WESTERN AUSTRALIA



Overview

- **Limitations imposed by the propagation medium on (sub)mm-VLBI observations.**
- **Multi-Frequency Calibration techniques to overcome them and widen the applicability of mm-VLBI.**
 - 1) SOURCE FREQUENCY PHASE REFERENCING (SFPR)
 - 2) MULTI FREQUENCY PHASE REFERENCING (MFPR)
- **Observational Demonstration and Measurements made possible by those techniques**
- **Instruments for multi-frequency observations**

The Many Faces of the Propagation Medium

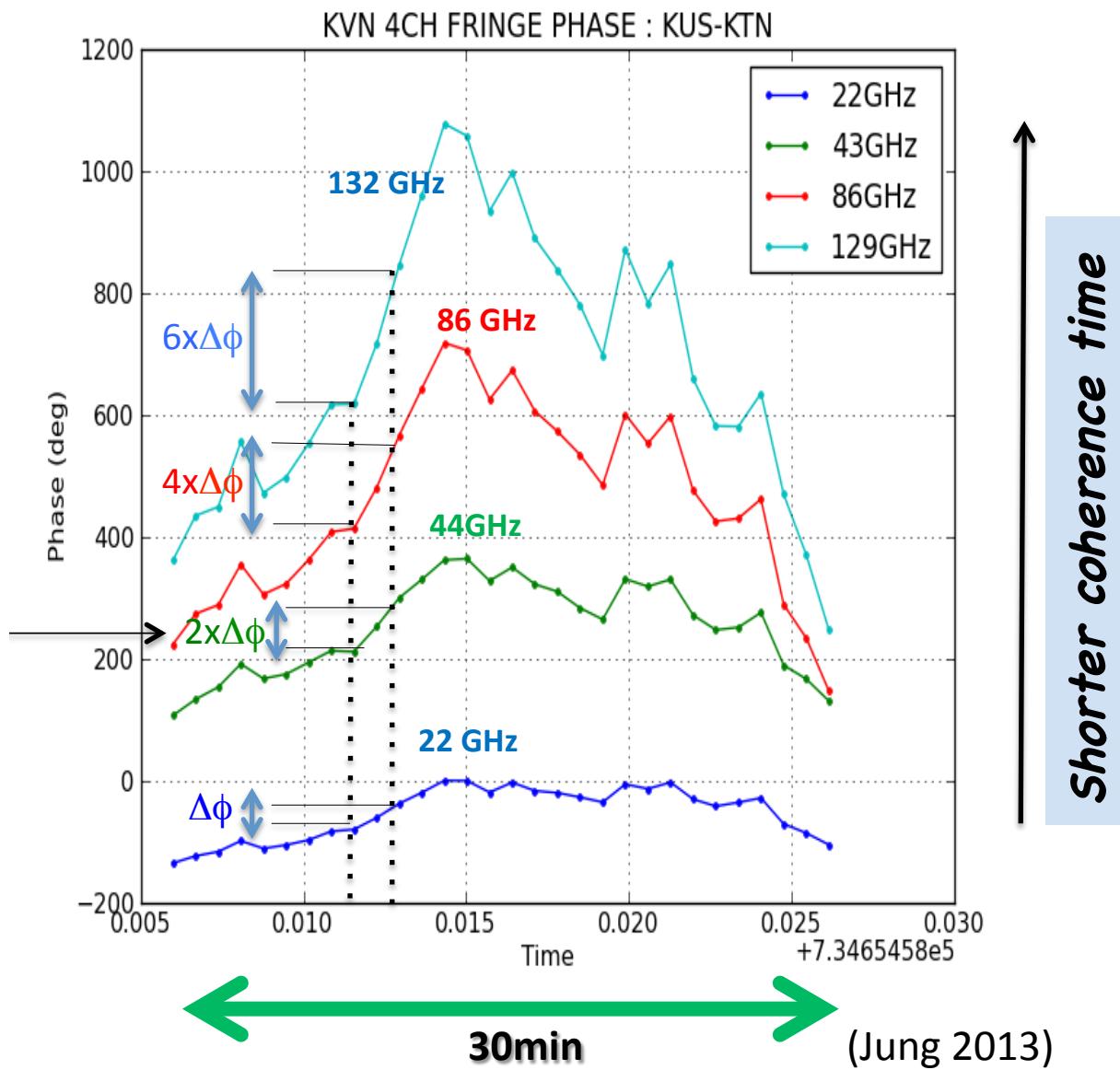


Troposphere "in action"

TROPOSPHERE
(non dispersive)

$$\tau_{\text{TRO}} = C$$

$$\Phi_{\text{TRO}} \propto v$$



Troposphere "in action"

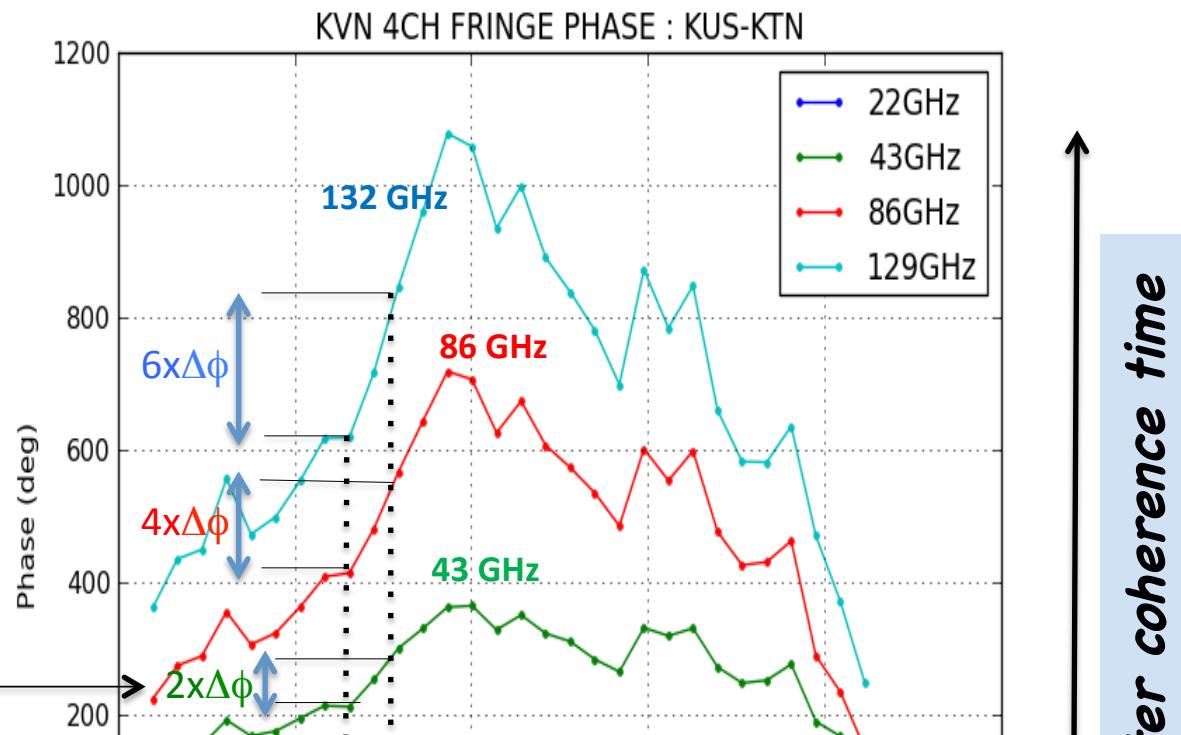
Fluctuations in water vapor component → phase fluctuations

TROPOSPHERE
(non dispersive)

$$\tau_{\text{TRO}} = C$$

$$\Phi_{\text{TRO}} \propto v$$

$$R = 44 / 22$$



Minimum Flux Detectable:

$$\Delta S_{ij} = \frac{1}{\eta_s} \times \sqrt{\frac{SEFD_i \times SEFD_j}{2 \times \Delta\nu \times \tau_{acc}}}$$

22 Ultimately prevents the application
of PHASE REFERENCING techniques for
-Weak source detection and
-Astrometric measurements.

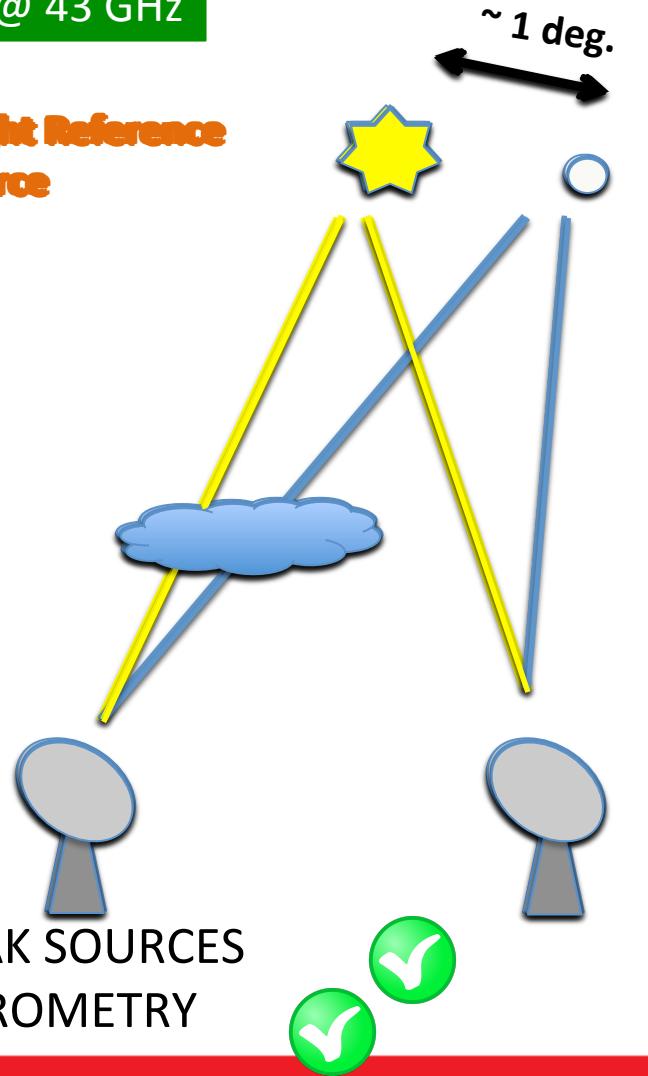
30min

(Jung 2013)

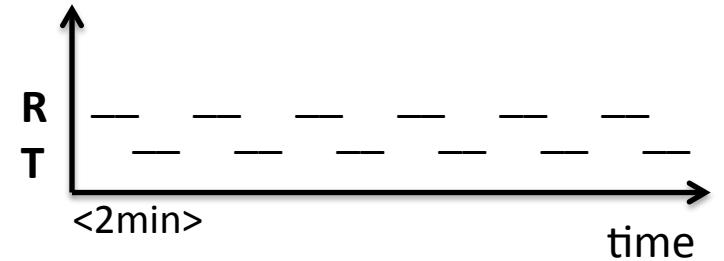
Phase Referencing “trans-source”

PR @ 43 GHz

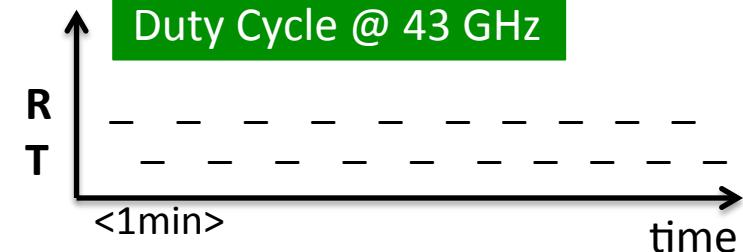
Bright Reference Source



Duty Cycle @ 22 GHz



Duty Cycle @ 43 GHz



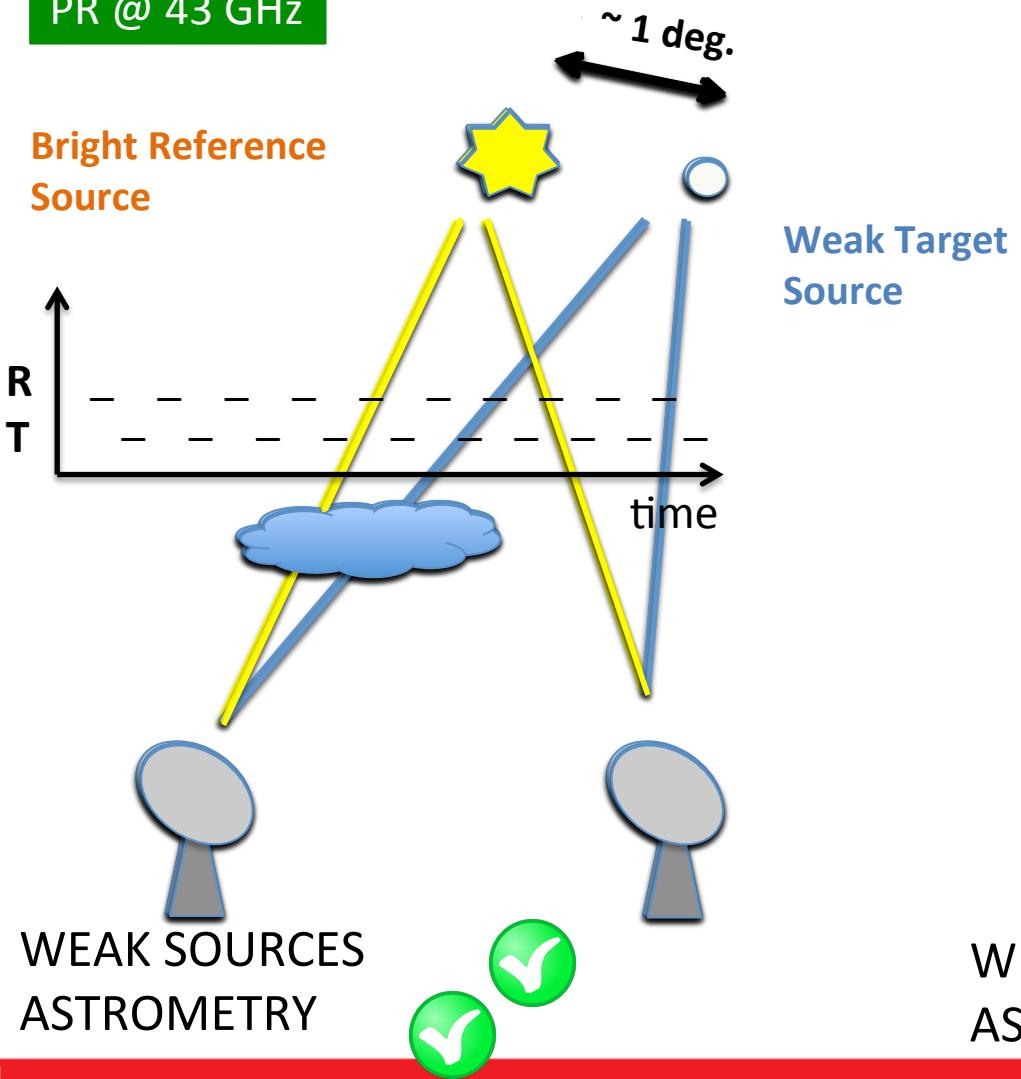
Limit on how fast a telescope can move constrains
The application to 43 GHz or below (in general).

Defeated by rapid phase tropospheric fluctuations,
linear increase with frequency (non-dispersive)

Limitations in performance start at freq. > 43 GHz

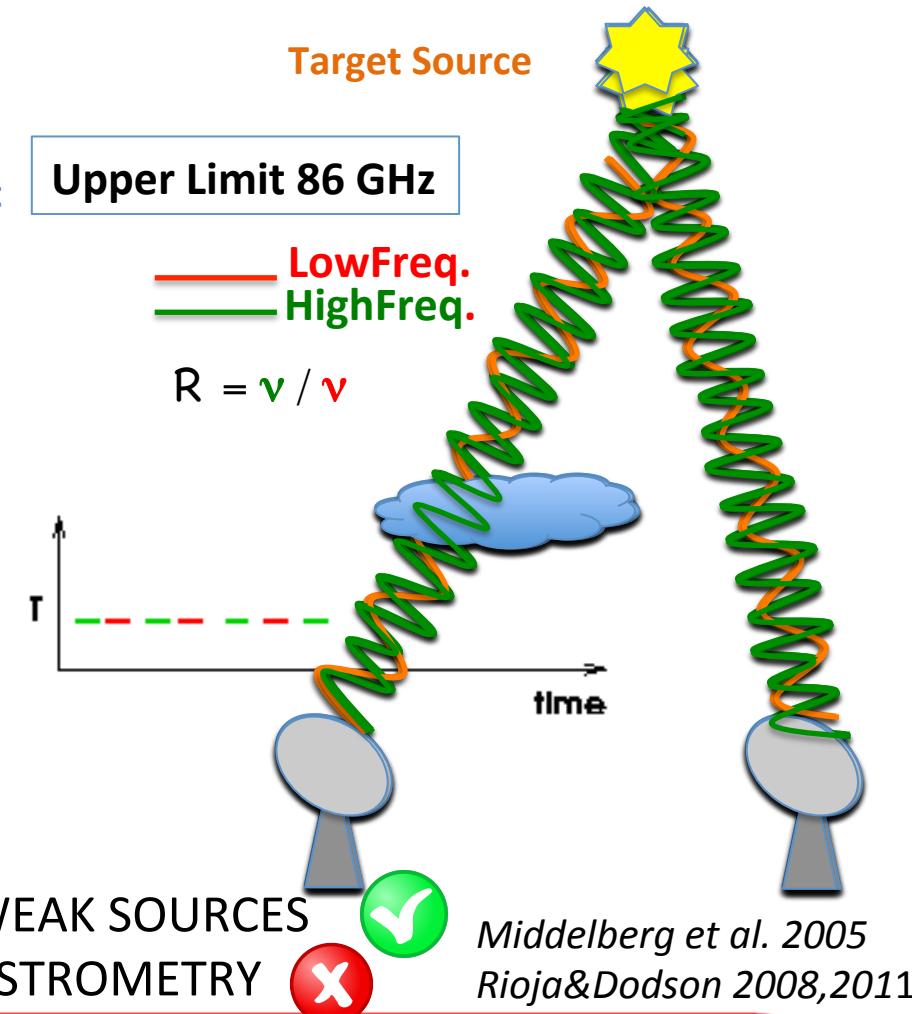
Phase Referencing “trans-source”

PR @ 43 GHz



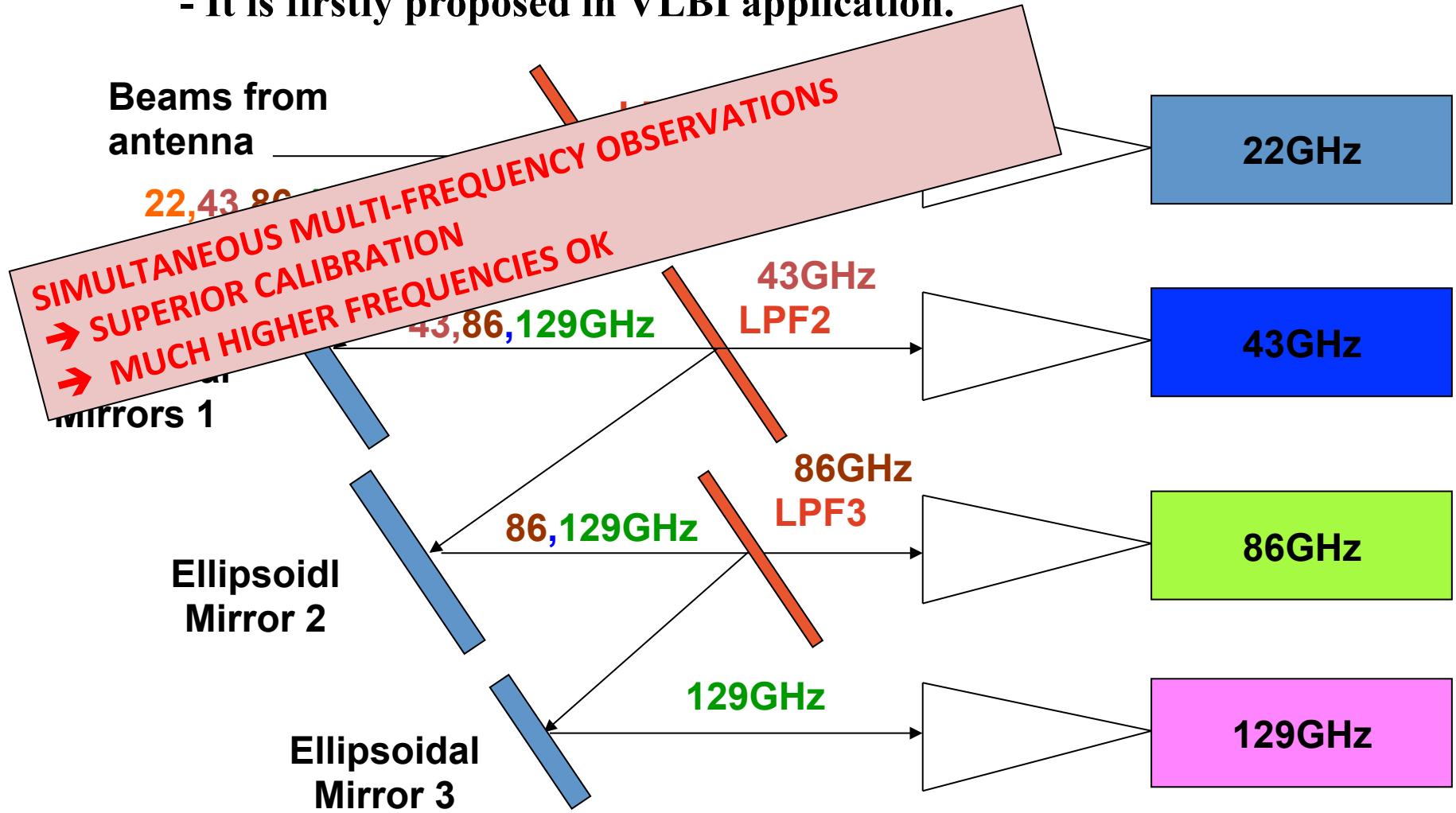
Paradigm Shift: “trans-frequency” calibration

“fast-frequency switching”
with VLBA



Multi-frequency receiving system of Korean VLBI Network (KVN)

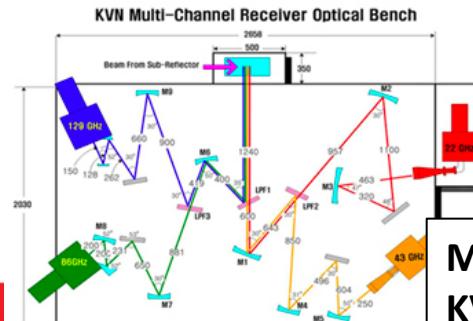
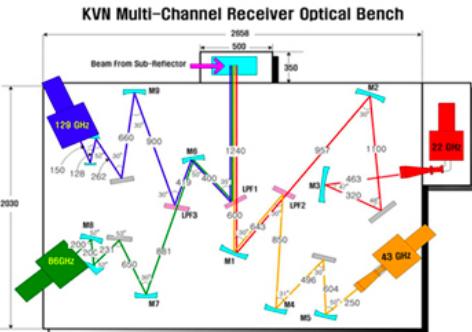
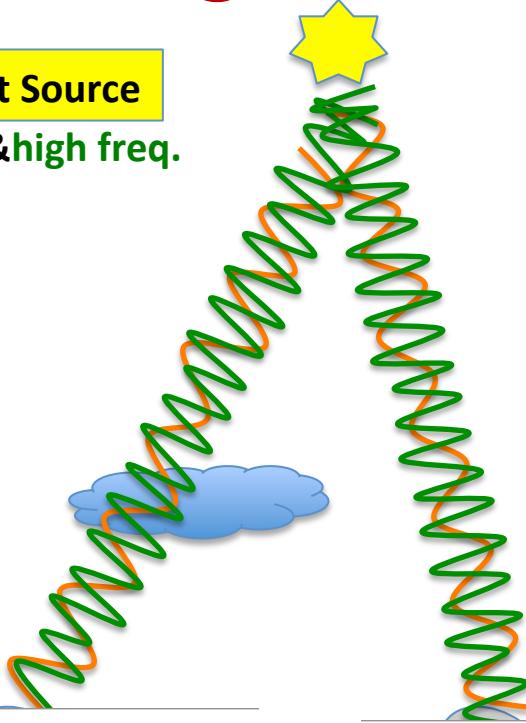
- Conceptual design came out **in April 2003**
- It is firstly proposed in VLBI application.



Frequency Phase Transfer (FPT)

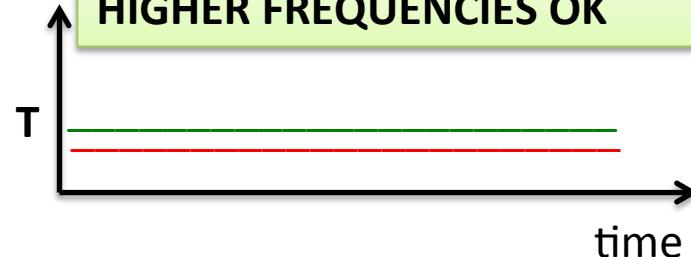
WEAK SOURCES
ASTROMETRY

Target Source
@low&high freq.



Multi-channel
KVN receivers

BETTER (near) SIMULTANEOUS!
HIGHER FREQUENCIES OK



$$R = \nu / \nu'$$

- 

$$\phi_A^{\text{FPT}} = \cancel{\phi_{\text{GEO}}} + \cancel{\phi_{\text{TRO}}} \quad \begin{matrix} \text{Fast} \\ \text{Slow} \end{matrix} \quad \begin{matrix} \text{Slow} \\ \text{Slow} \end{matrix}$$

$$\Phi_{\text{ION}} + \phi_{\text{INST}} + \phi'_{\text{A,STR}} + 2\pi n_A$$

$$R * \phi_A = R * (\phi_{A,\text{GEO}} + \phi_{A,\text{TRO}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + 2\pi n_A)$$

Non-dispersive Errors:

$$\phi_{A,\text{TRO}} - R * \phi_{A,\text{TRO}} = 0$$

$$\phi_{A,\text{GEO}} - R * \phi_{A,\text{GEO}} = 0$$



Dispersive Errors:

$$\phi_{A,\text{ION}} - R * \phi_{A,\text{ION}} = (R-1/R) * \phi_{A,\text{ION}}$$

$\phi_{\text{INST}} \dots$ Anything!





Frequency Phase Transfer (FPT)

OUTCOME: PRECISE CALIBRATION OF THE TROPOSPHERE
(and in general any non-dispersive residuals)

ENABLES: EXTENDED COHERENCE TIME

- WEAK SOURCE DETECTION AT HIGH FREQUENCIES
- ~~ASTROMETRY~~

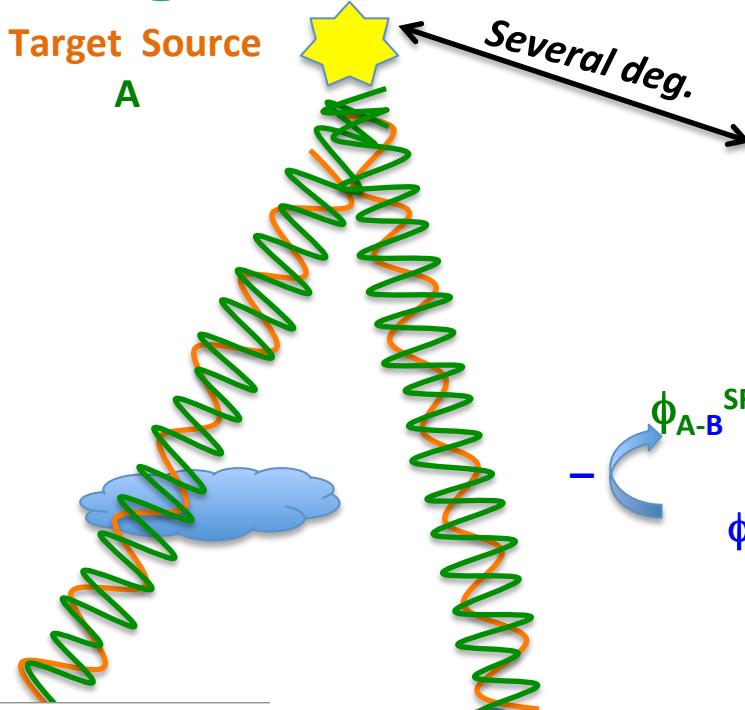
* (*near*) SIMULTANEOUS multi-frequency observations required for high freqs.



The Quest of Astrometry...

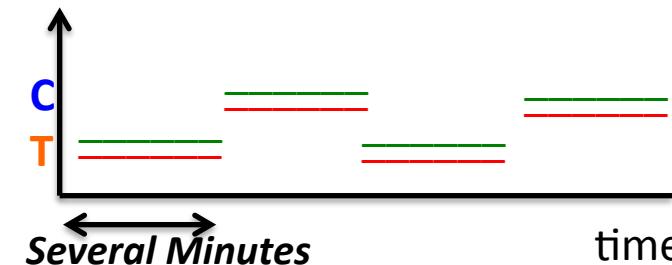
Source Frequency Phase Referencing (SFPR)

WEAK SOURCES
ASTROMETRY



SFPR: Rioja & Dodson '08, '11, '14, '15

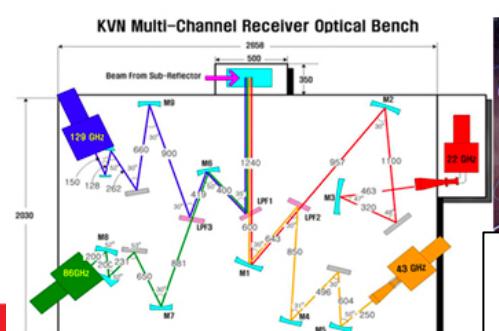
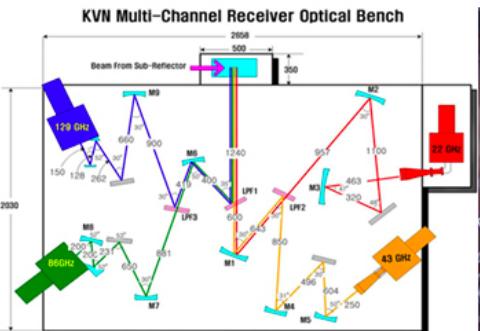
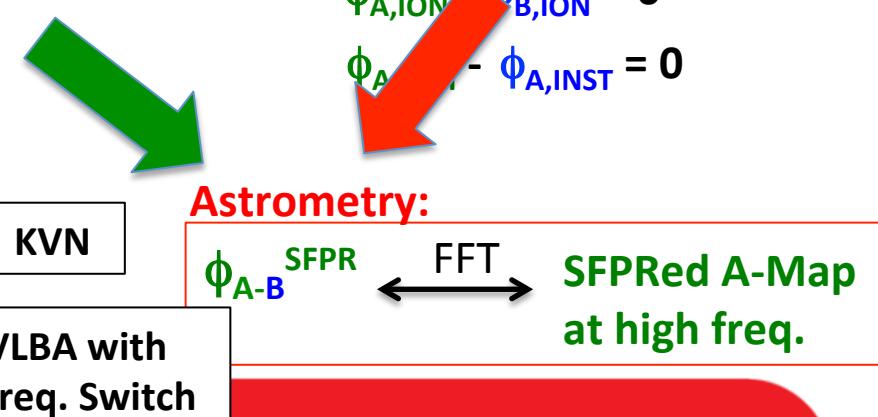
(TWO SOURCES)



$$R = v / v'$$

$$\begin{aligned}\phi_{A-B}^{\text{SFPR}} &= \phi_{A,\text{EO}} + \phi_{A,\text{O}} + \phi_{A,\text{N}} + \phi_{A,\text{STR}} + 2\pi n_A \\ \phi_B^{\text{FPT}} &= \phi_{B,\text{EO}} + \phi_{B,\text{O}} + \phi_{B,\text{ION}} + \phi_{B,\text{INST}} + \phi_{B,\text{STR}} + 2\pi n_B\end{aligned}$$

$$\begin{aligned}\phi_{A,\text{ION}} - \phi_{B,\text{ION}} &= 0 \\ \phi_A - \phi_{A,\text{INST}} - \phi_{B,\text{INST}} &= 0\end{aligned}$$



Source Frequency Phase Referencing (SFPR)

OUTCOME: PRECISE ATMOSPHERIC & INSTR. CALIBRATION,
WHILE KEEPING ASTROMETRIC SIGNATURE

ENABLES: EXTEND COHERENCE TIME & ASTROMETRY AT HIGH FREQS

TARGET SCIENCE:

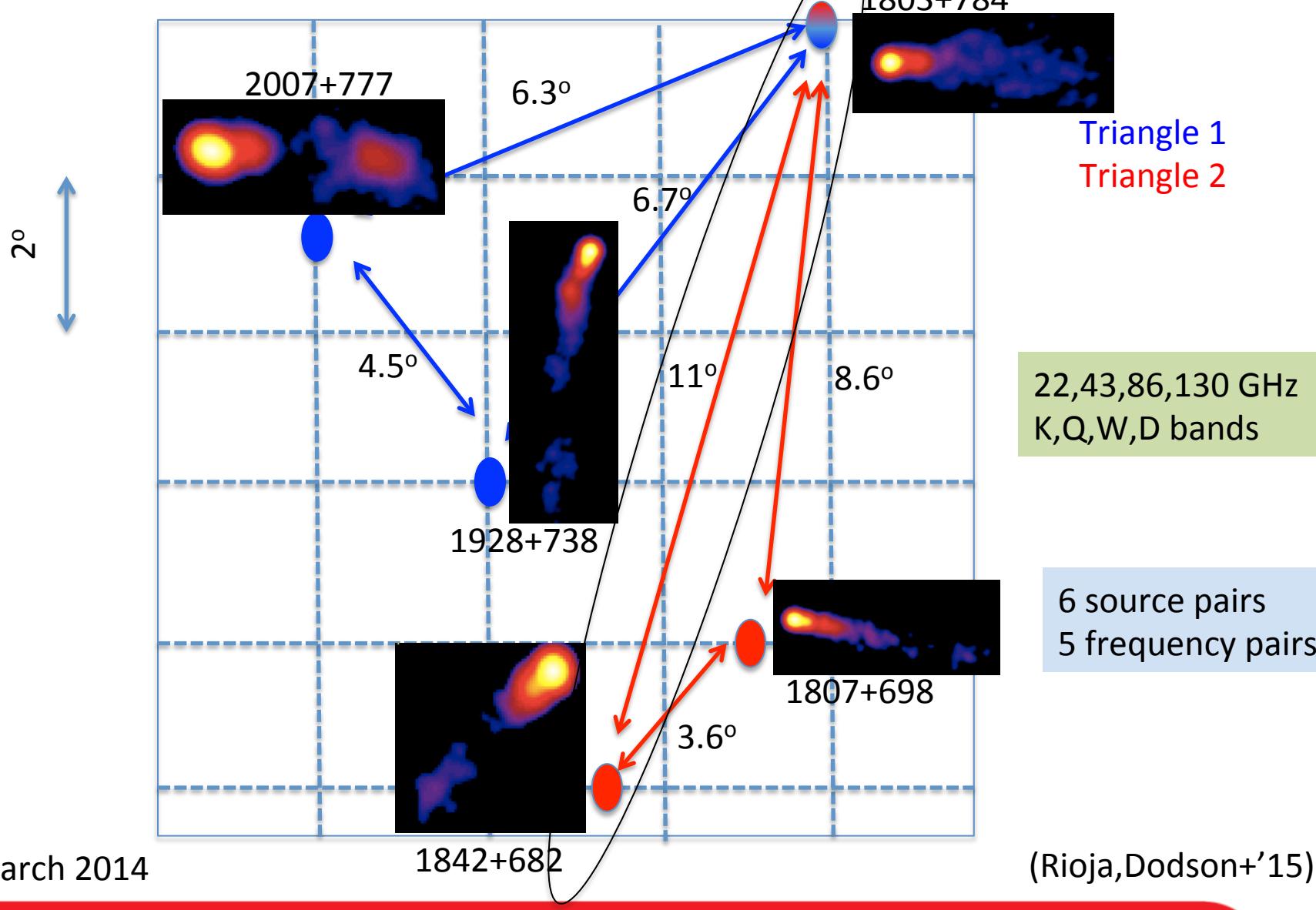
- ➔ WEAK SOURCE DETECTION
- ➔ ASTROMETRY (chromatic astrometry: continuum & line
Registration of images at multiple frequencies:
Spectral index maps,
AGN “core-shifts”;
Faraday Rotation (polarization))

*Slow antenna switching OK

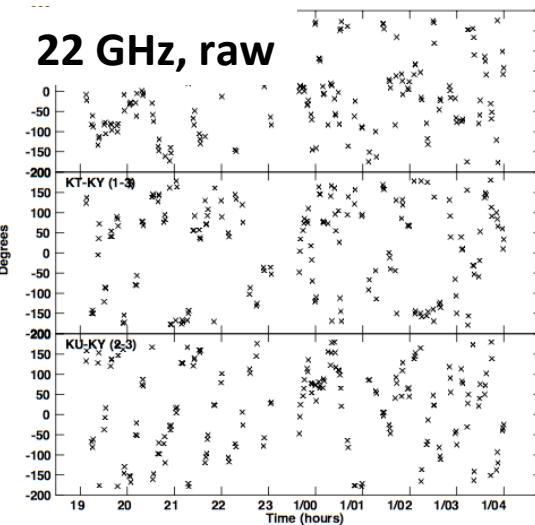
*Several degrees source separation OK

* *(near)SIMULTANEOUS multi-frequency observations required for high freqs.*

Empirical Demonstration: 4-band KVN SFPR observations of 5 AGNs

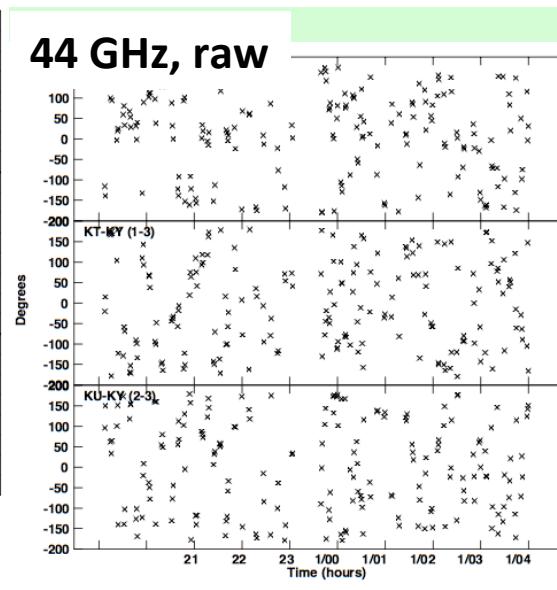


22 GHz, raw

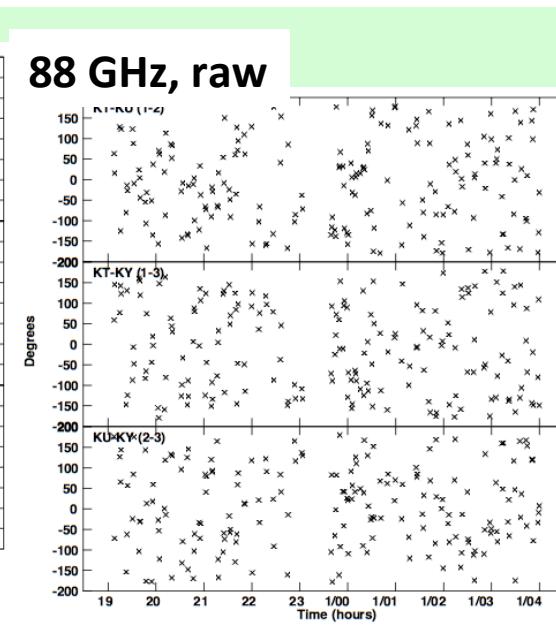


$$\phi_A = \phi_{A,\text{GEO}} + \phi_{A,\text{TRO}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + 2\pi n_A$$

44 GHz, raw

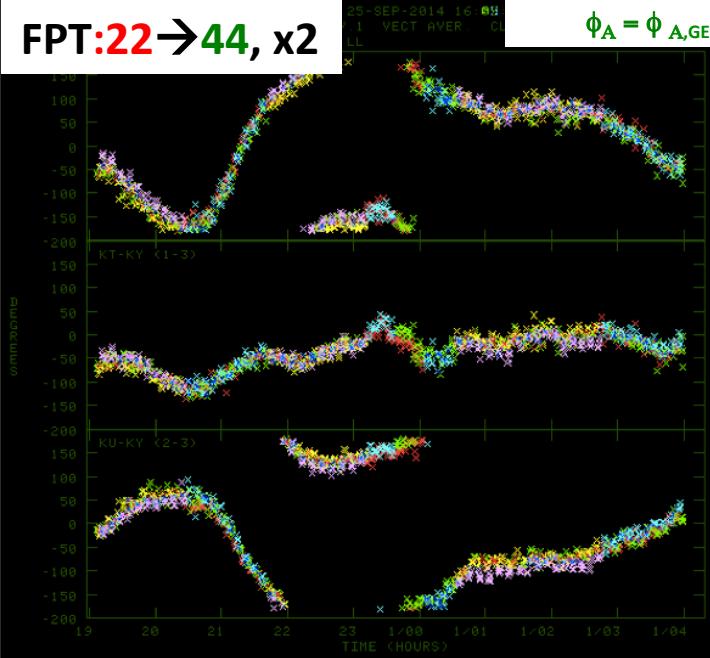


88 GHz, raw



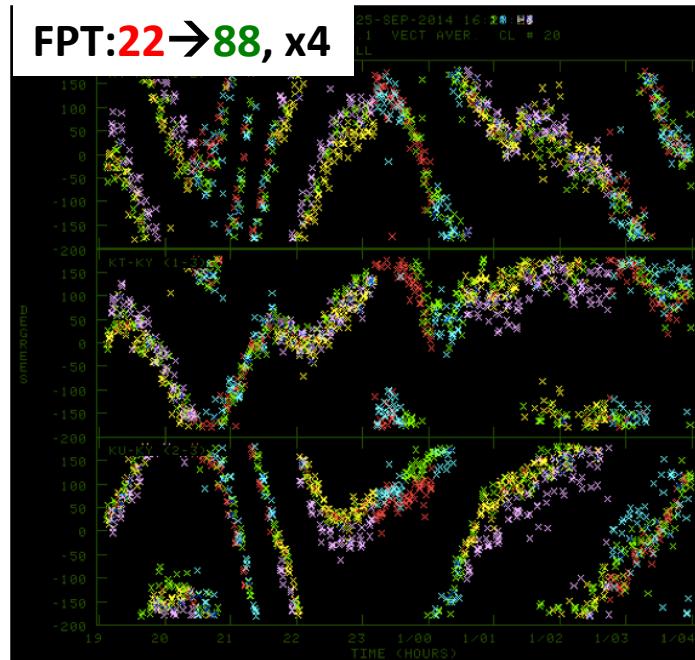
Hz)

FPT:22 → 44, x2



$$\phi_A - 2 * \phi_A$$

FPT:22 → 88, x4

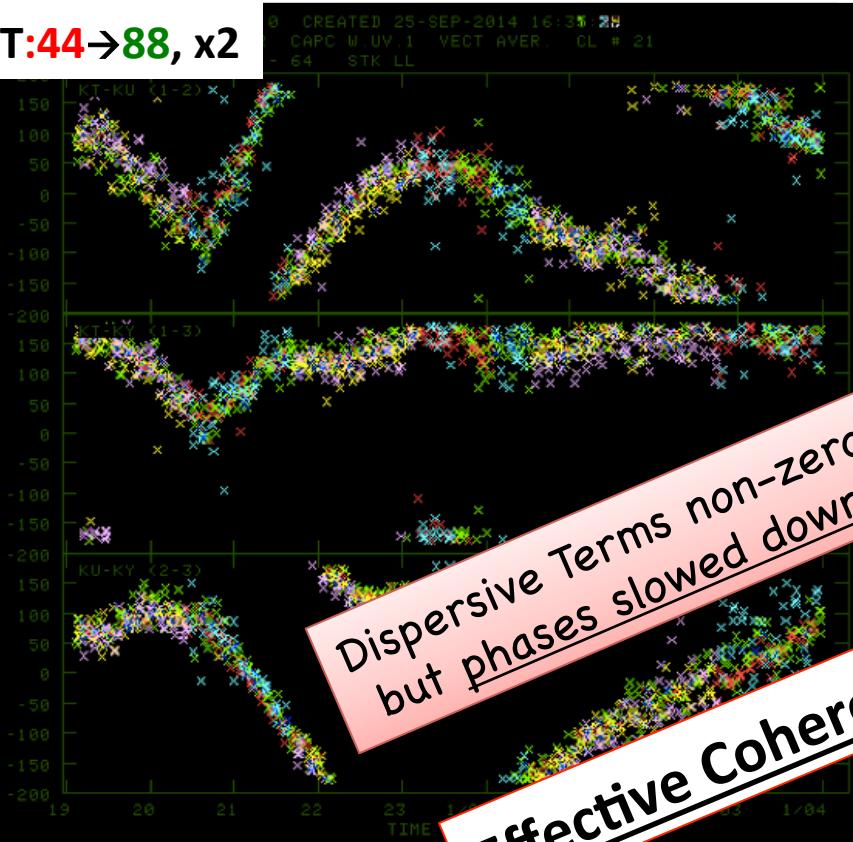


$$\phi_A - 2 * \phi_A$$

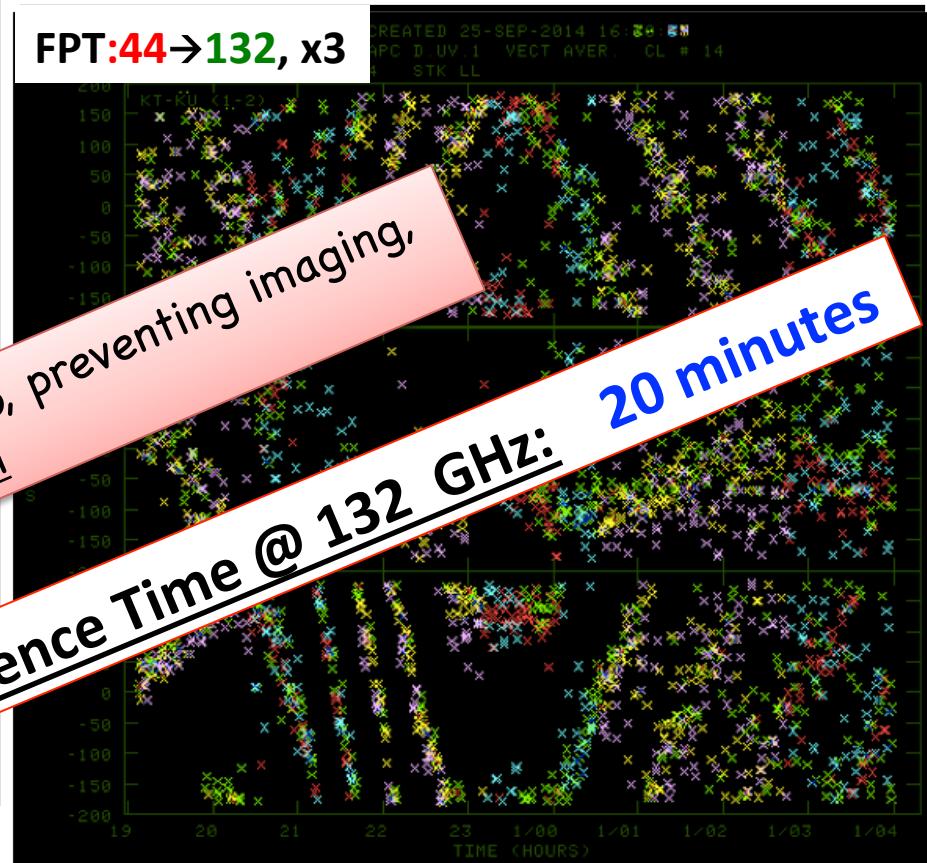
FPT analysis – “2-frequencies”

Residuals increase with R, for a given ν_{low} (44 GHz)

FPT:44→88, x2



FPT:44→132, x3



Dispersive Terms non-zero, preventing imaging,
but phases slowed down

Effective Coherence Time @ 132 GHz:

20 minutes

$$R = \nu / \nu'$$

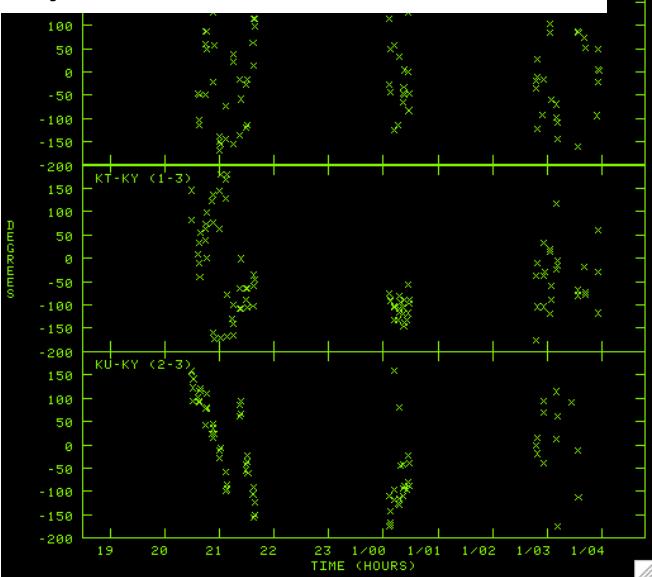
Fast Slow Slow

$$\phi_A^{\text{FPT}} = \cancel{\Phi}_{\text{GEO}} + \cancel{\Phi}_{\text{TRO}} + \Phi_{\text{ION}} + \phi_{\text{INST}} + \phi'_{A,\text{STR}} + 2\pi n_A$$

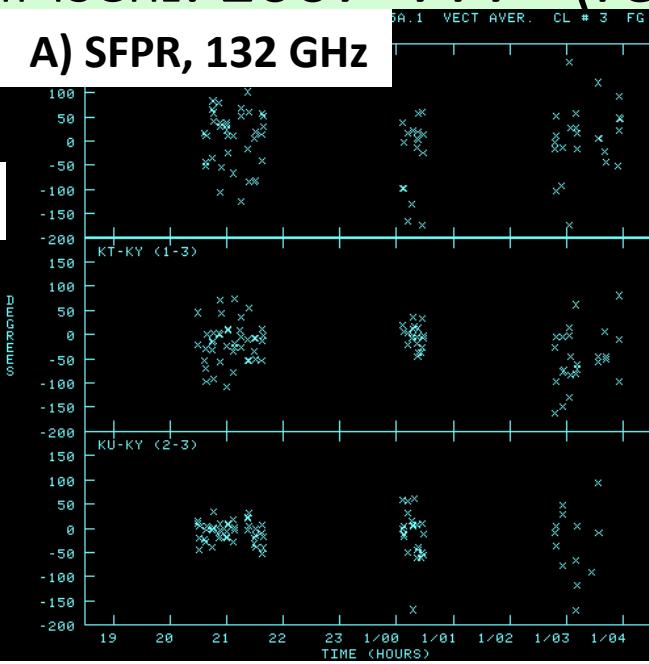
$$R * \phi_A = R * (\phi_{A,\text{GEO}} + \phi_{A,\text{TRO}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + 2\pi n_A)$$

SFPR analysis – 132 GHz with 43GHz: 2007+777 (ref. 6.3° away)

A) 2007+777, FPT, 44→132, x3



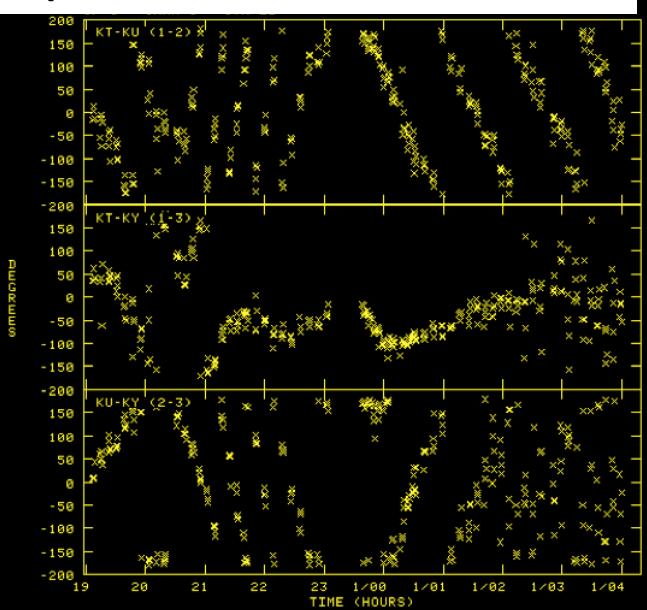
A) SFPR, 132 GHz



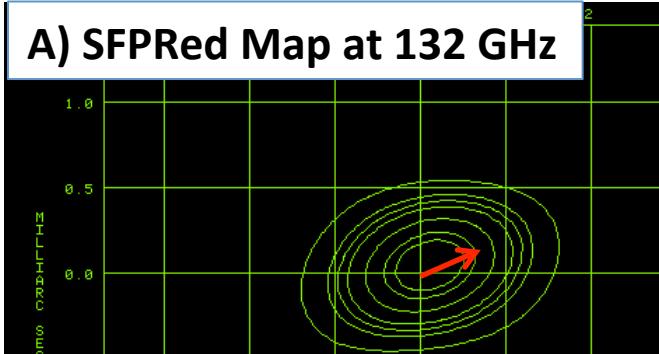
A) – B)

Effective Coherence Time @132 GHz:
8 hours

B) 1803+784, FPT, 44→132, x3

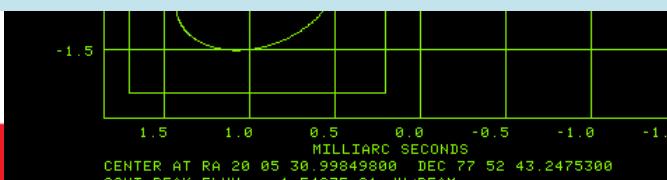


A) SFPRed Map at 132 GHz



Peak Flux ~ 150 mJy
rms ~ 5mJy/beam
85-90% Flux Recovery

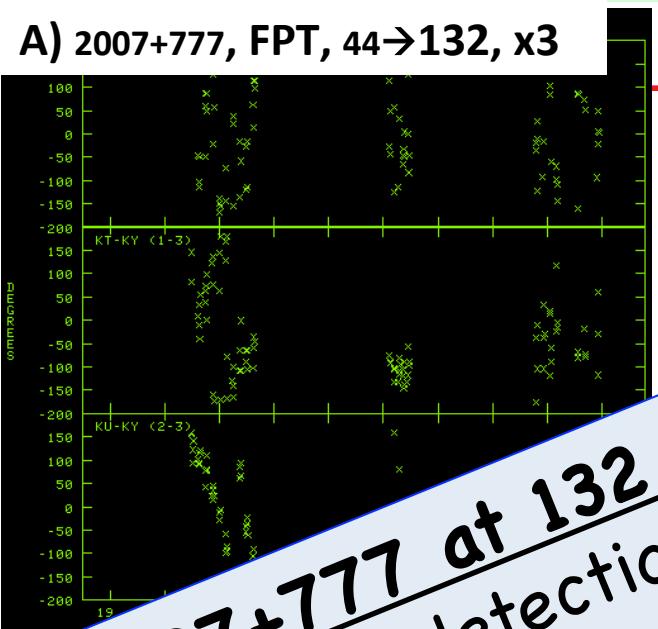
Bona-fide Astrometry Measurement
Frequency Dependent Position Shift ~ (-50,+50) μas



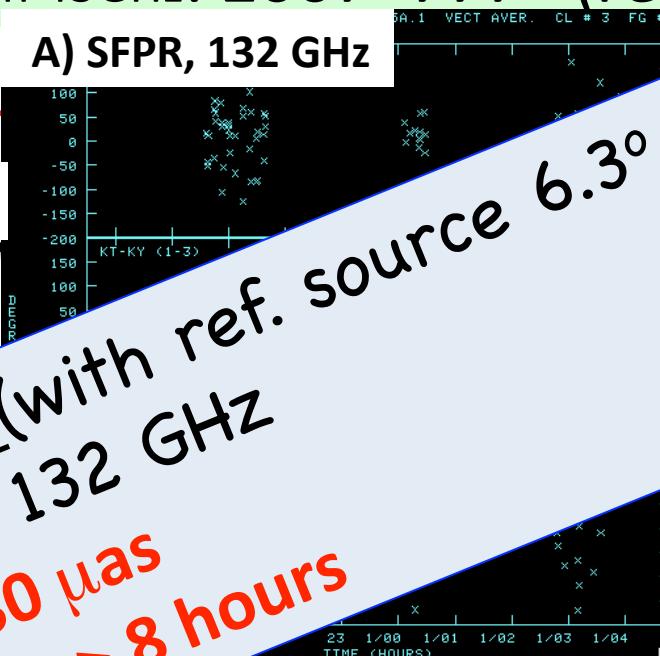
CENTER AT RA 20 05 30.99849800 DEC 77 52 43.2475300

SFPR analysis – 132 GHz with 43GHz: 2007+777 (ref. 6.3° away)

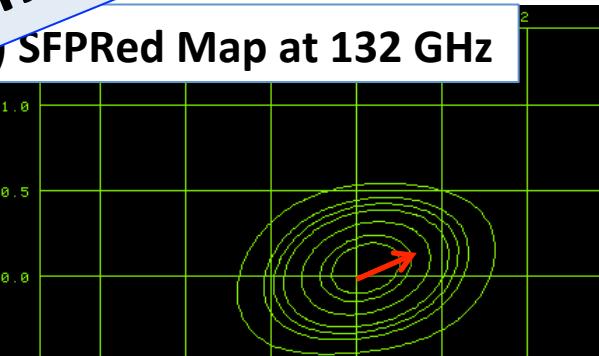
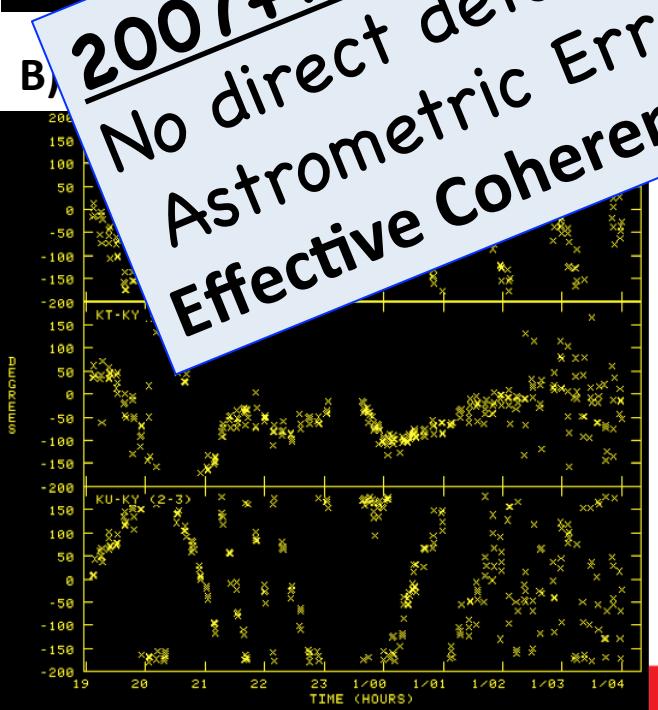
A) 2007+777, FPT, 44→132, x3



A) SFPR, 132 GHz

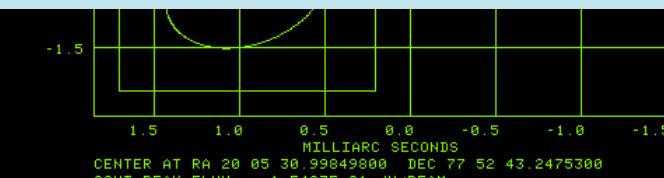


A) - B)



Peak Flux ~ 150 mJy
rms ~ 5mJy/beam
85-90% Flux Recovery

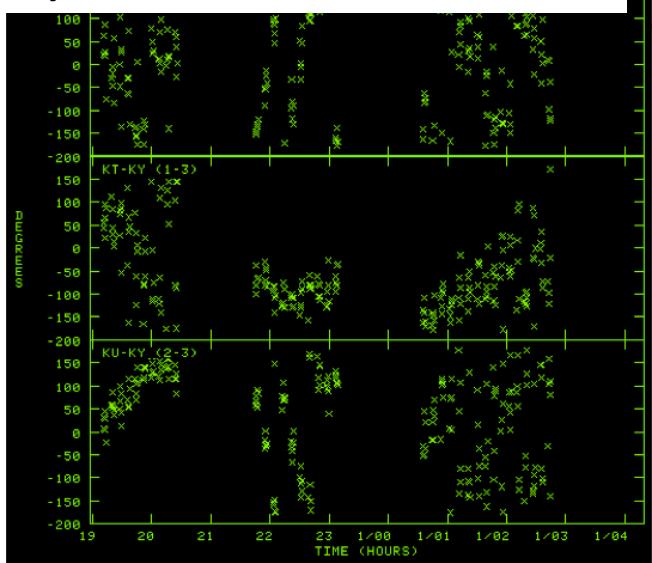
Bona-fide Astrometry Measurement
Frequency Dependent Position Shift ~ (-50,+50) μ as



FFT

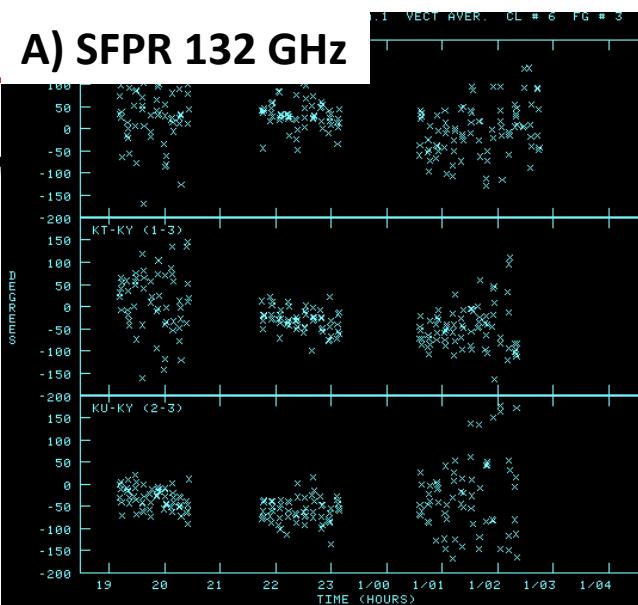
SFPR analysis – 132 GHz with 43GHz: 1842+681 (ref. 11° away)

A) 1842+681 FPT, 44 → 132, x3



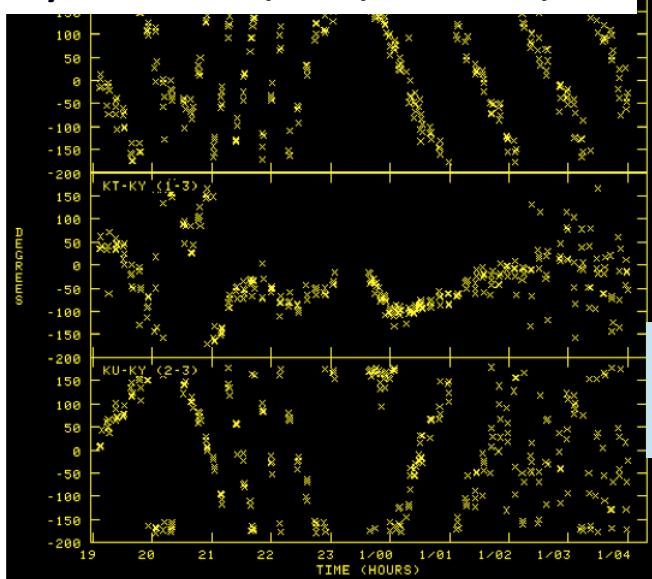
A) – B)

A) SFPR 132 GHz



FFT

B) 1803+784, FPT, 44 → 132, x3

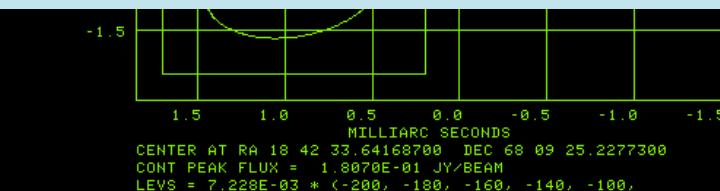


A) SFPRed Map at 132 GHz



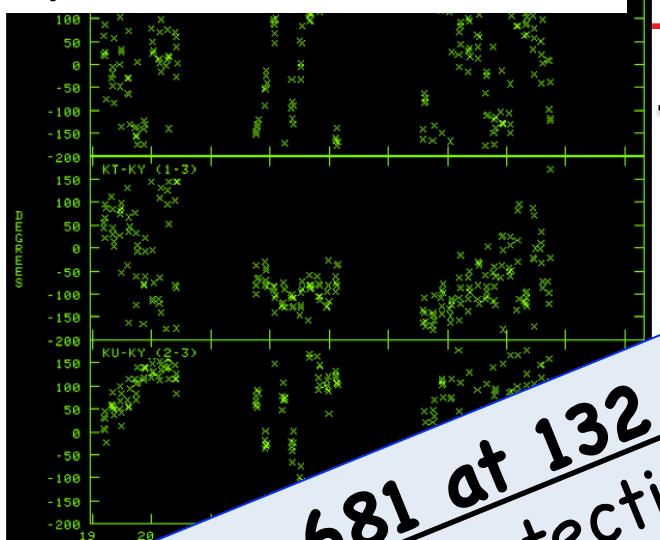
Peak Flux ~ 100 mJy
rms ~ 5 mJy/beam
87% Flux Recovery

**Bona-fide Astrometry Measurement
Frequency Dependent Position Shift ~ (-221,+150) μas**



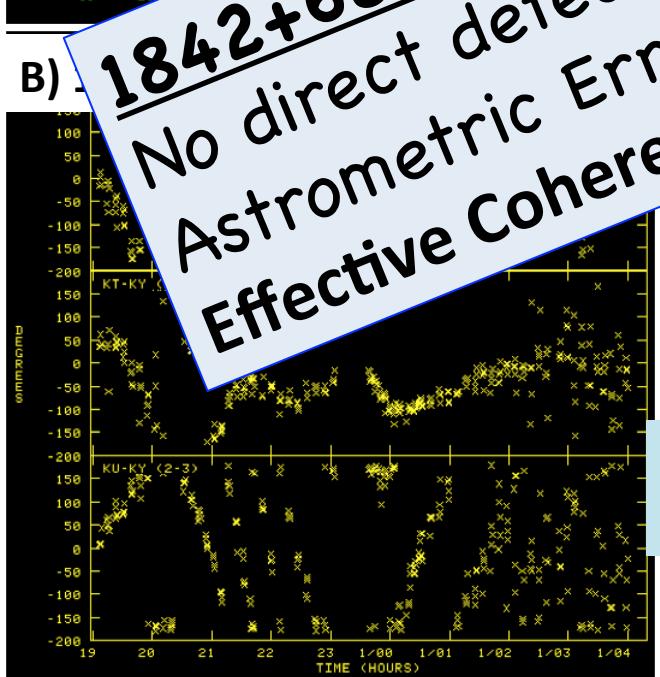
SFPR analysis – 132 GHz with 43GHz: 1842+681 (ref. 11° away)

A) 1842+681 FPT, 44 → 132, x3



A) SFPR 132 GHz

A) - B)

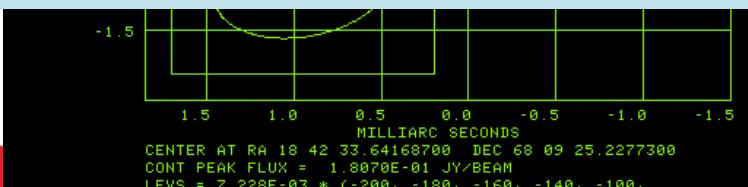


**No direct detections at 132 GHz
Astrometric Error ~ 50 μas
Effective Coherence Time > 8 hours**



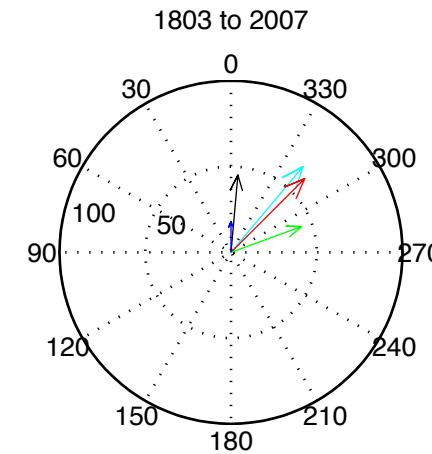
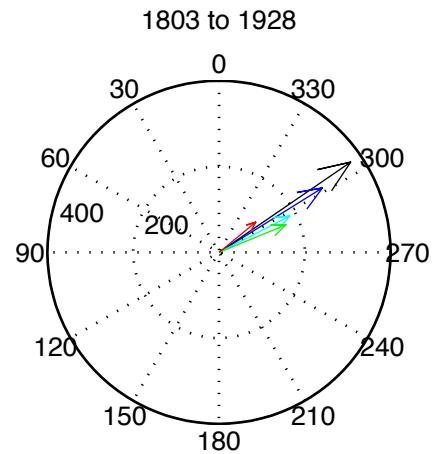
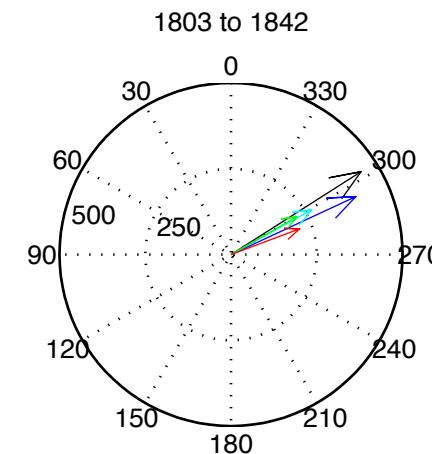
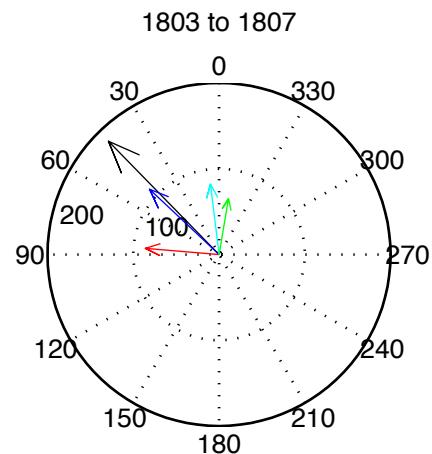
Peak Flux ~ 100 mJy
rms ~ 5 mJy/beam
87% Flux Recovery

**Bona-fide Astrometry Measurement
Frequency Dependent Position Shift ~ (-221,+150) μas**



↔ FFT

SFPR Astrometric RELATIVE Measurements: between TWO frequencies & TWO sources



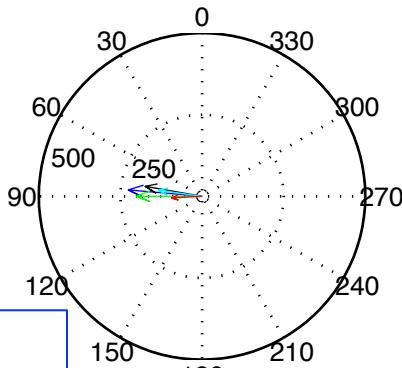
Red-KQ
Blue KW
Black KD
Green QW
Cyan QD

Individual Source Shifts: Singular Value Decomposition Method PLUS Alignment with Jet Direction Constraint

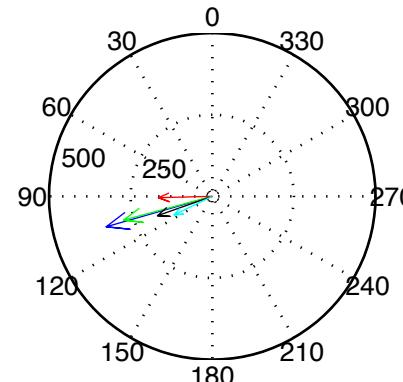


Red KQ
Blue KW
Cyan KD
Green QW
Black QD

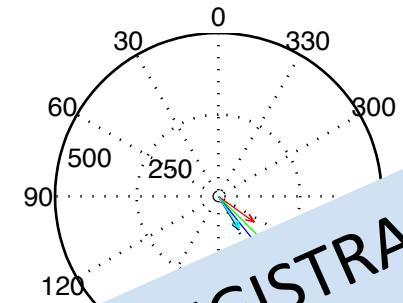
1803+784



1807+698

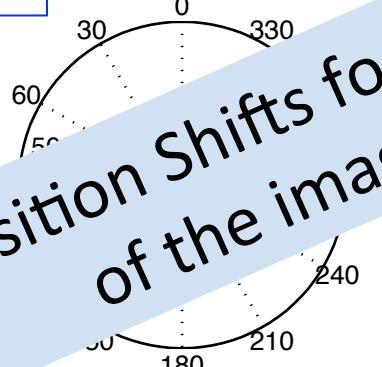


1842+681



Non-Degenerate Solution

1928+738



Position Shifts for "bona fide" astrometric REGISTRATION
of the images of each AGN at the four frequency bands.

Jet Directions

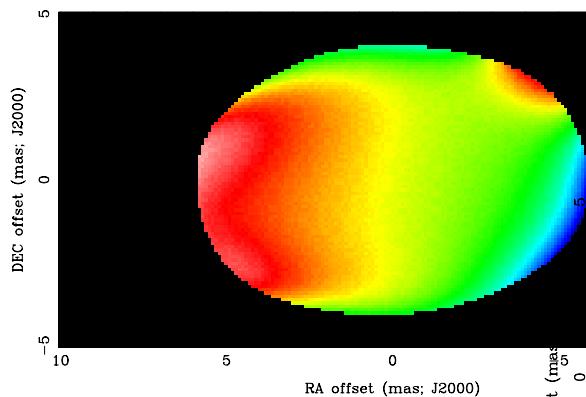
**1803+784
1807+698
1842+681**

1928+738

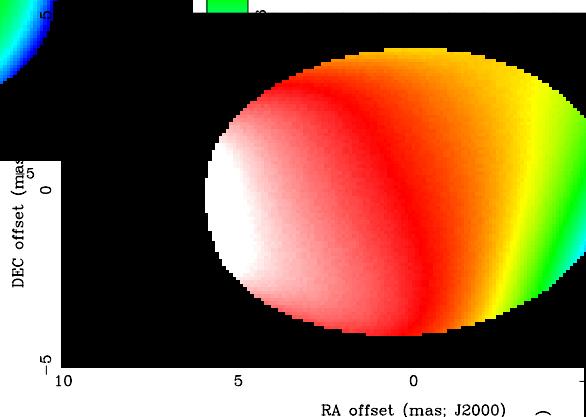
Spectral Index Maps: Astrometrically Aligned Images



22/43 GHz

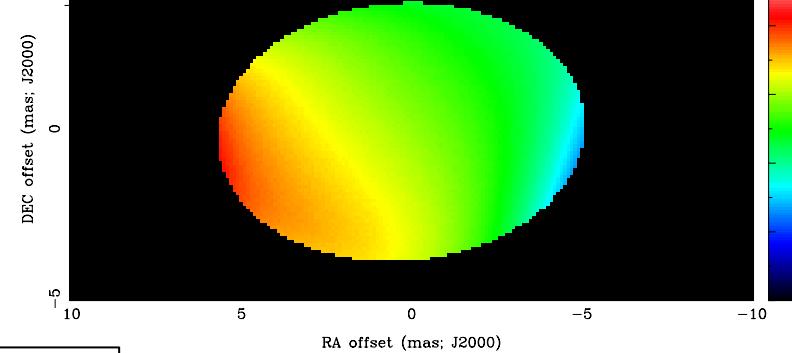


22/86 GHz



1807+698

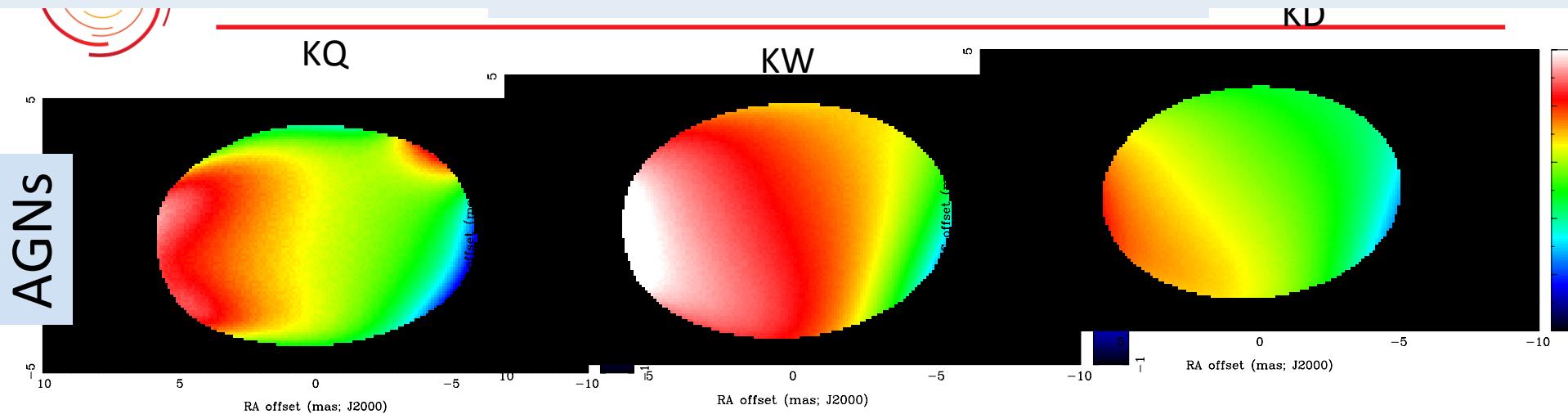
22/132 GHz



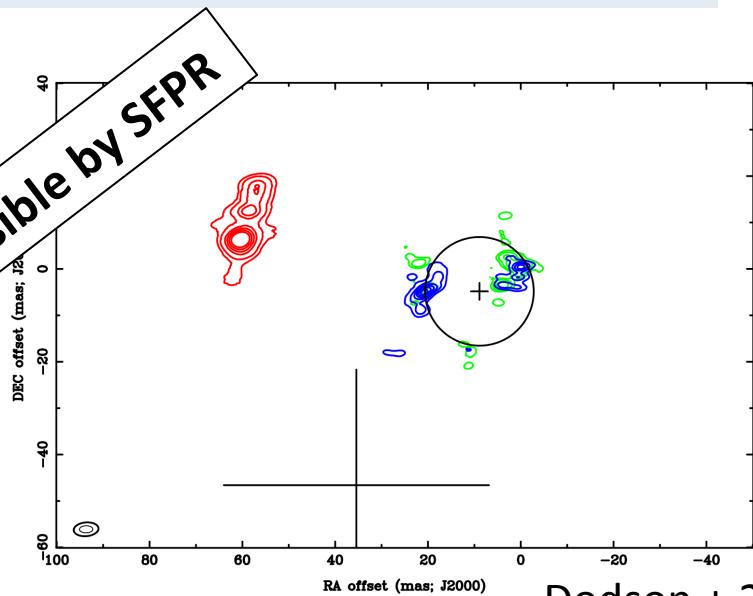
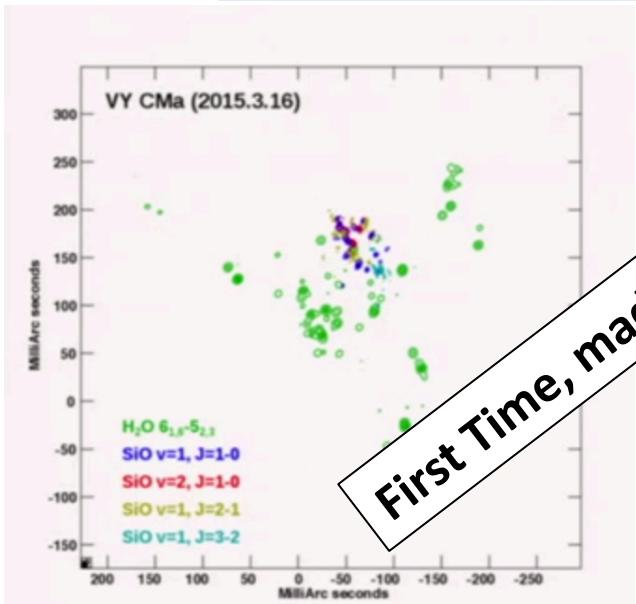
**First Time “bona fide” Astrometry at 132 GHz,
Made possible by SFPR**

*On-going developments
towards a high resolution
multi-freq array (x-KVN)*

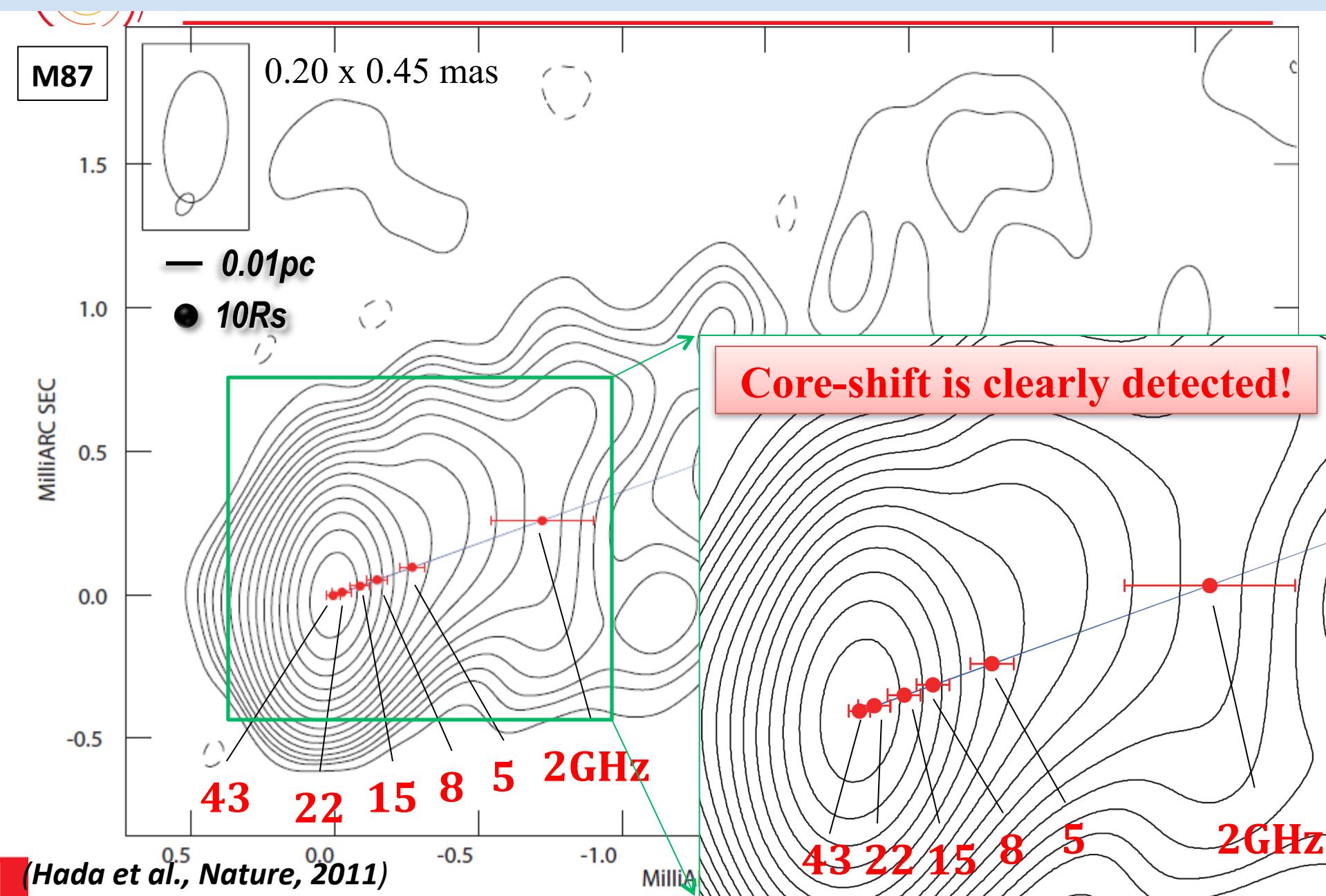
Spectral Index Maps: Astrometrically Aligned Images



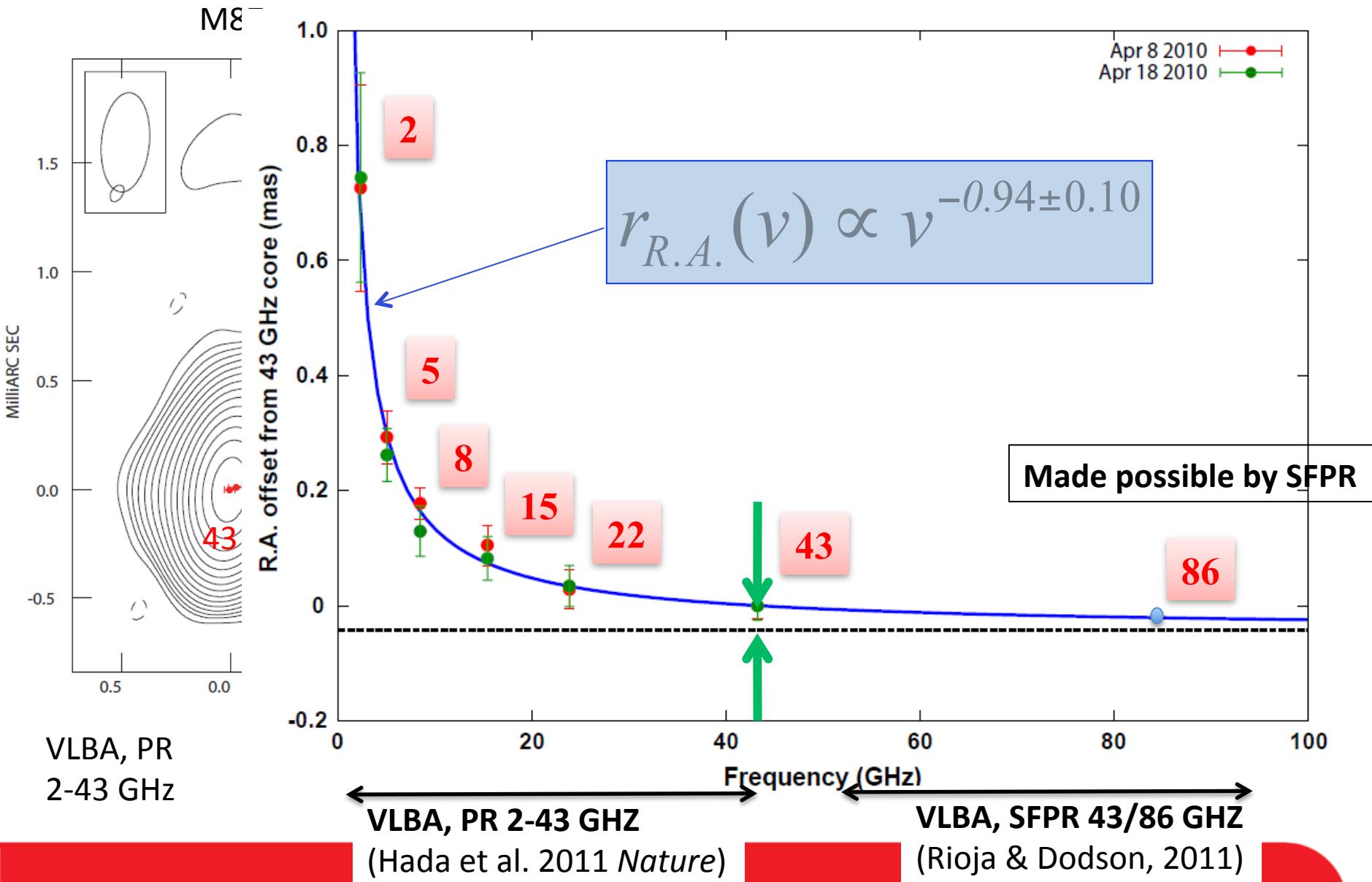
Registration of multi-transition masers



AGN Core-Shift Measurements (Optical Depth)



AGN: Multi Frequency astrometry



Developments for mm-VLBI continue... ICE blocks



ICE = Ionospheric Extraction

Multi Frequency Phase Referencing (MFPR) Technique: a variation of SFPR, with a **SINGLE** source

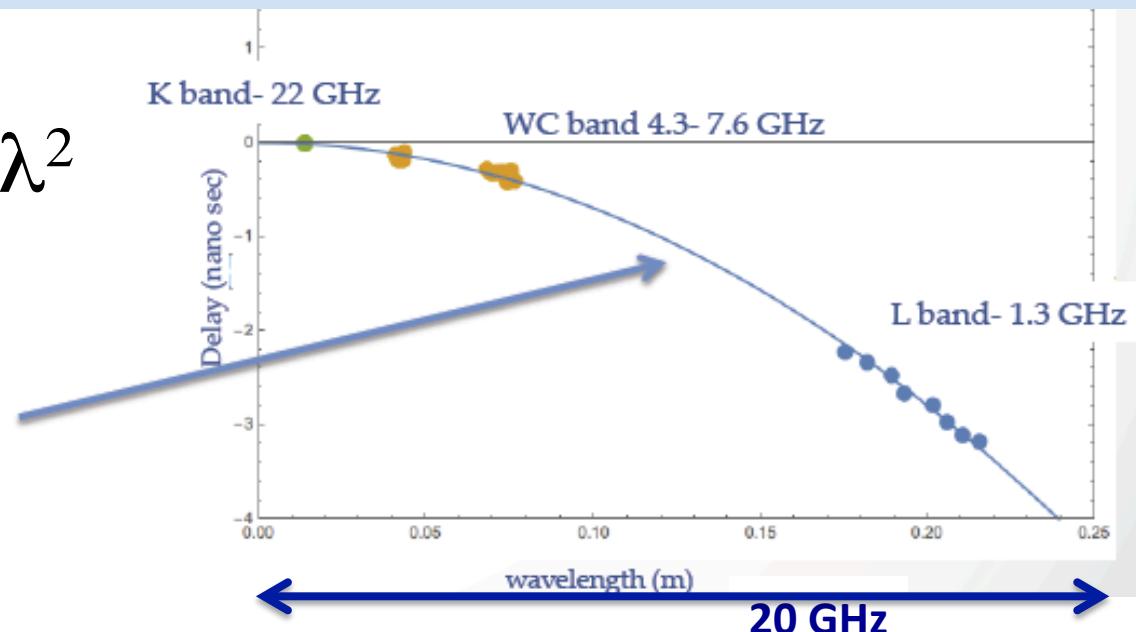
Trop. Delay is same at all λ 's
(non-dispersive)

$$\delta \tau = c + 1.34 \Delta \text{TEC} \cdot \lambda^2$$

Tec (Total electron content)

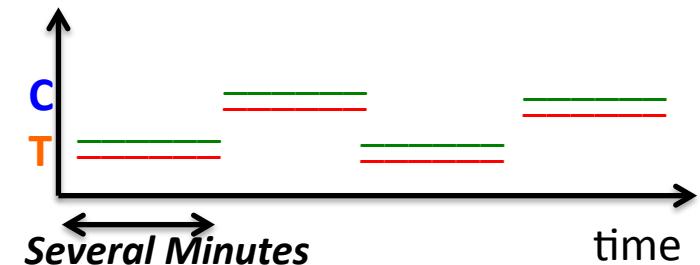
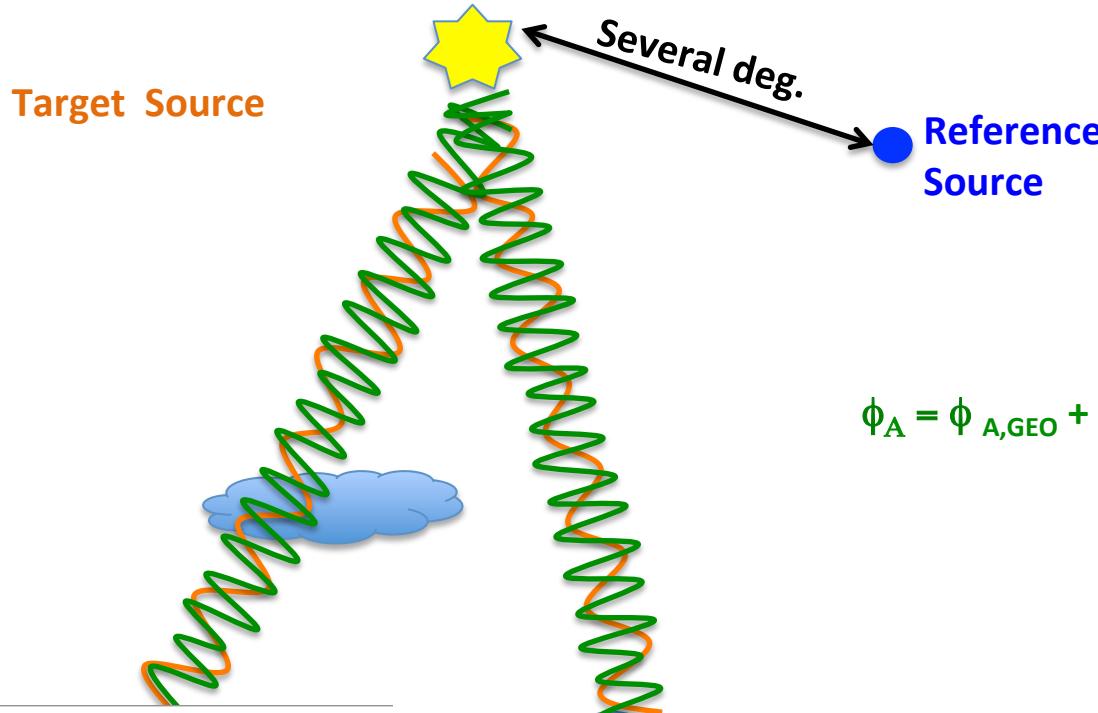
We have developed a program to fit the data.

ICE Blocks: Fast-alternating multi frequency observations
at low frequencies, of the target source.



Source Frequency Phase Referencing

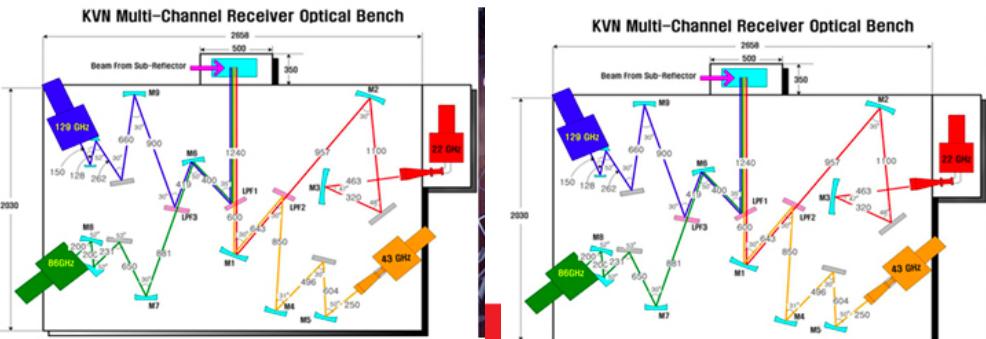
Two Sources, Two Frequencies



$$R = \nu / \nu$$

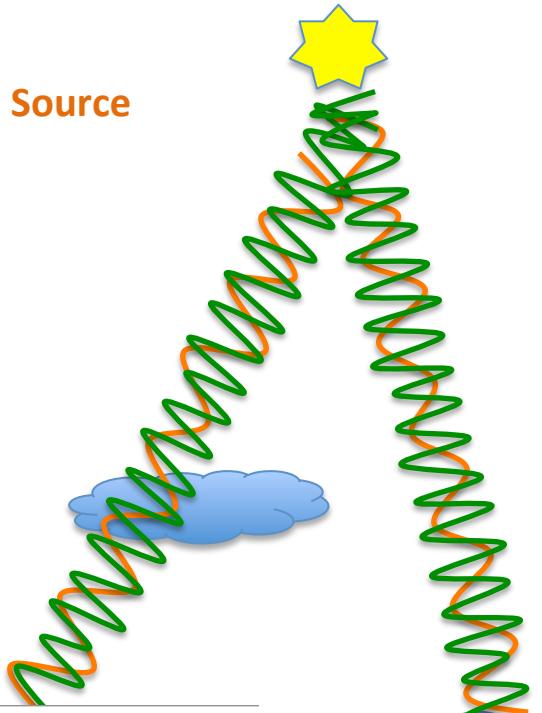
Fast Slow Slow

$$\phi_A = \phi_{A,\text{GEO}} + \phi_{A,\text{TRO}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + \phi_{A,\text{STR}} + 2\pi n_A$$

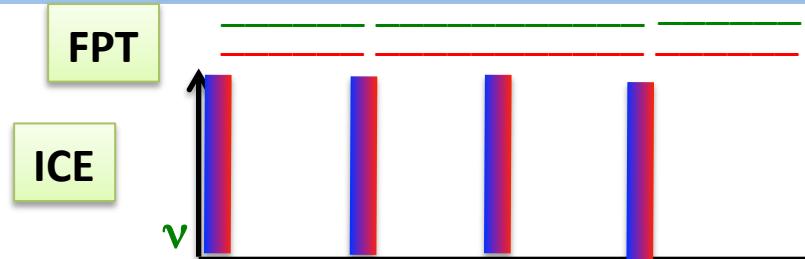


Multi-Frequency Phase Referencing (MFPR)

Target Source

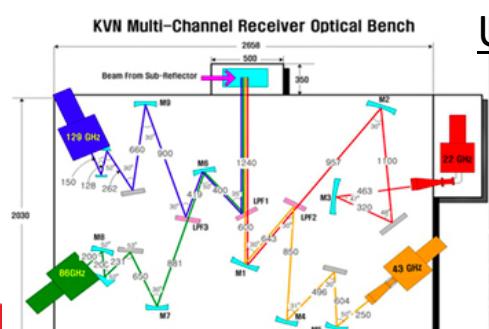
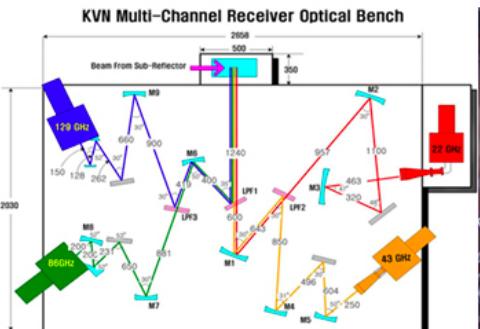


Single Source, Multi-Frequency



$$R = v / \nu$$

$$\begin{aligned} \phi_A &= \phi_{\text{ion}} + \phi_{\text{FPT}} + \phi_{\text{ICE}} + \phi_{\text{STR}} + \phi_{\text{A,INST}} + 2\pi n_A \\ \text{Fast} &\quad \text{Slow} \quad \text{Slow} \\ \text{FPT} &\quad \text{ICE} \\ \phi_{\text{A,ION}} &= f\text{TEC}(v) \rightarrow \Delta\text{TEC} \end{aligned}$$



Use primary calibrator for $\phi_{\text{A,INST}}$ = stable (cte).

Multi-Frequency Phase Referencing (MFPR)



Basics of Multi-Frequency Phase Referencing (single source)

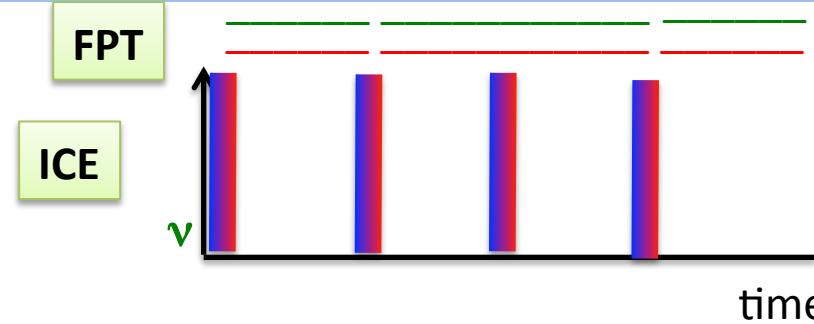
Use multi-frequency observations to derive TEC, i.e. the Ionospheric contribution

- 'Curvature' of delay as a function of freq. allows determination of Δ TEC

Use fast frequency-switching to derive non-dispersive terms, i.e. the Tropospheric contribution

- Use solutions from 'easy' low freq.
- Scale phase by freq ratio

Single Source, Multi-Frequency



$$R = v / v$$

$$\phi_A = \phi_{A,ION} + \phi_{A,TRO} + \phi_{A,STR} + \phi_{A,INST} + 2\pi n_A$$
$$\phi_{A,ION} = fTEC(v) \rightarrow \Delta TEC$$

Use primary calibrator for $\phi_{A,INST}$ = stable (cte).



Multi-Frequency Phase Referencing (MFPR)



Basics of Multi-Frequency Phase Referencing (single source)

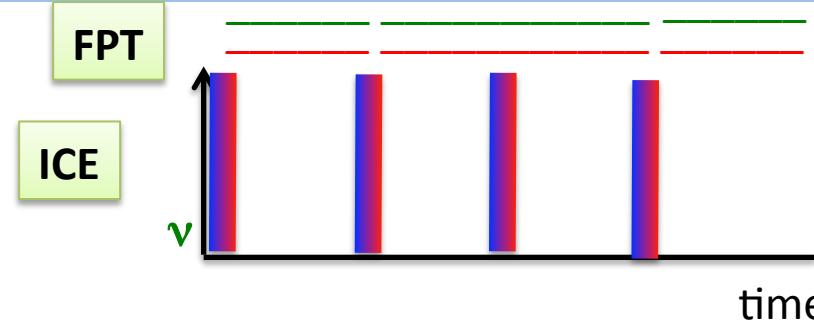
Use multi-frequency observations to derive TEC, i.e. the Ionospheric contribution

- 'Curvature' of delay as a function of freq. allows determination of Δ TEC

Use fast frequency-switching to derive non-dispersive terms, i.e. the Tropospheric contribution

- Use solutions from 'easy' low freq.
- Scale phase by freq ratio

Single Source, Multi-Frequency



$$R = v / v$$

$$\phi_A = \phi_{A,ION} + \phi_{A,TRO} + \phi_{A,STR} + \phi_{A,INST} + 2\pi n_A$$
$$\phi_{A,ION} = fTEC(v) \rightarrow \Delta TEC$$

Use primary calibrator for $\phi_{A,INST}$ = stable (cte).



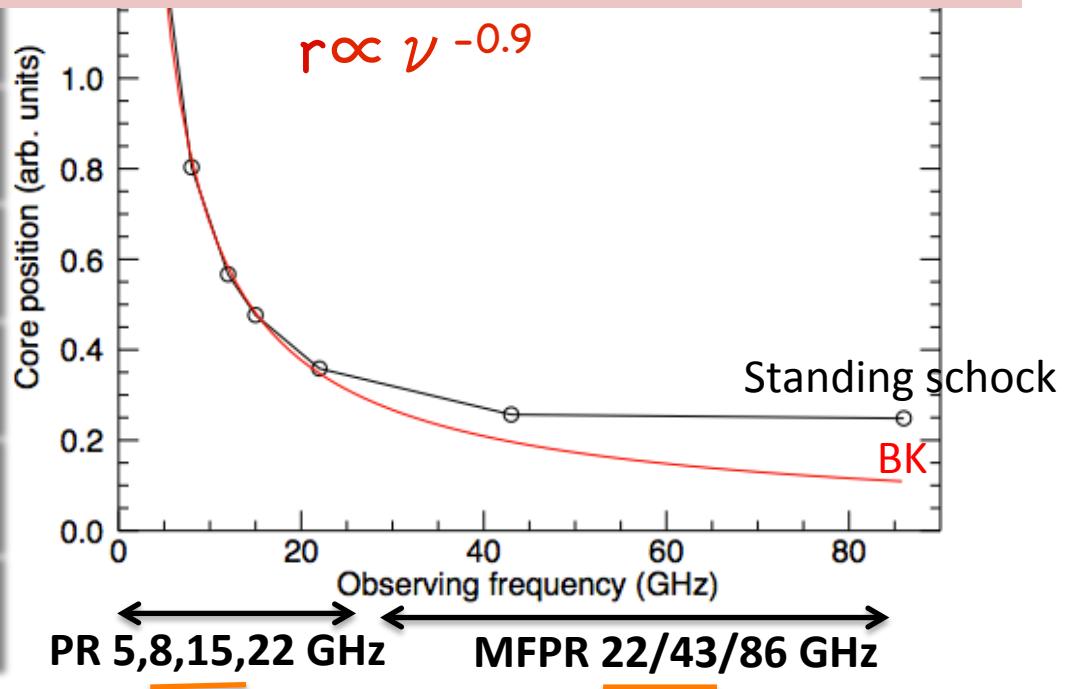
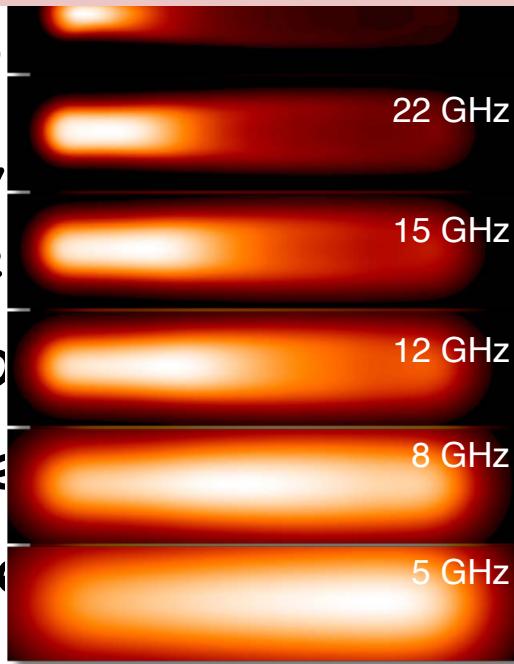
Blazar “Core Shifts” at mm-wavelengths (Optical Depth, Standing Shocks?)

There are many reasons (particularly the association of gamma ray & radio flares Marscher, Nature ‘12) to believe that in Blazars there are standing shocks at which the B&K model breaks-down
And these should be revealed at the higher frequencies where conventional PR is not possible.

Blazar “Core Shifts” at mm-wavelengths (Optical Depth, Standing Shocks?)

High precision astrometry at high frequencies could distinguish between both
→ VLBA program of observations of blazars to elucidate the nature of the
radio core in AGNs

association
Marscher,
there are
breaks-do
And these
frequencies



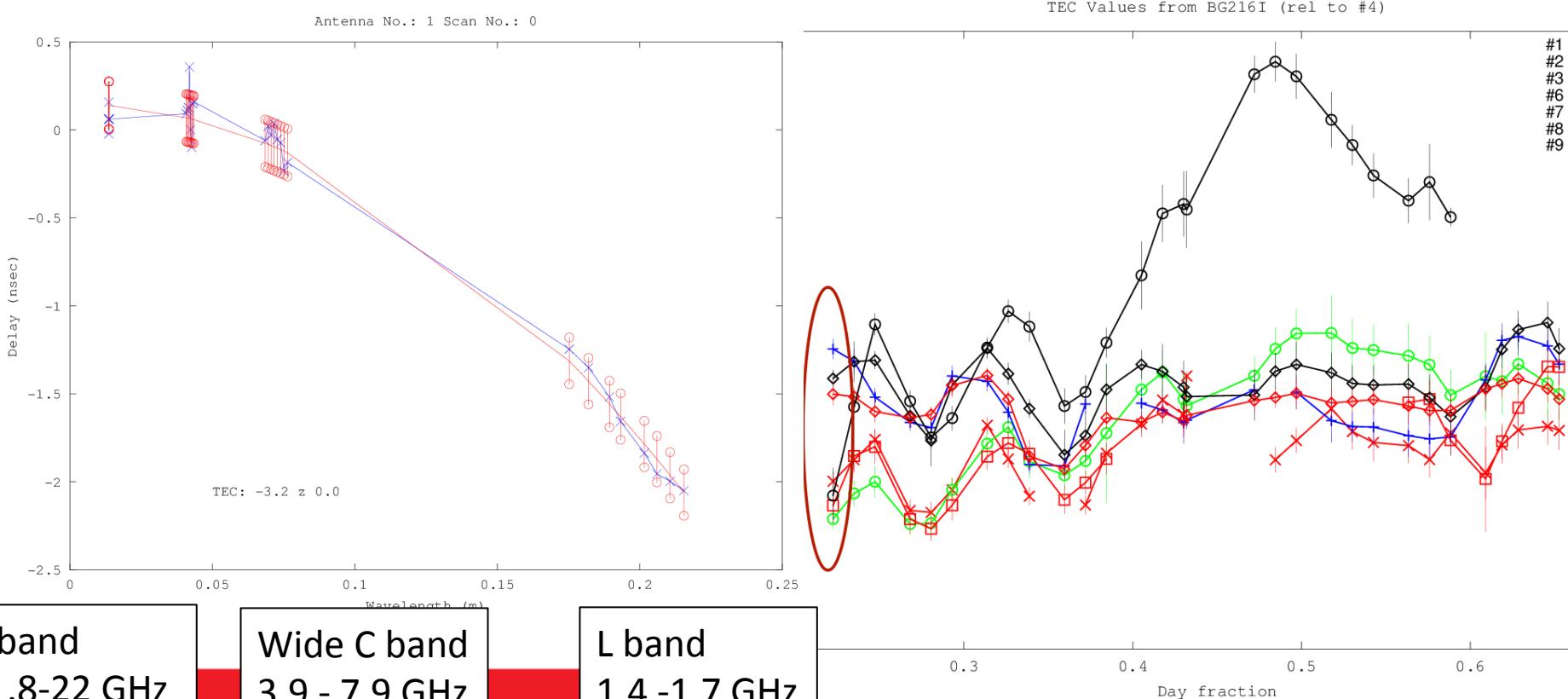
Left: Sync. emission from RMHD models (JLGomez; J.Marti)

Right: Expected core-shifts for this class of AGN (black) vs BK (red)

Experiment BG216I – BL Lac

Solve for delays (per IF) across all frequencies

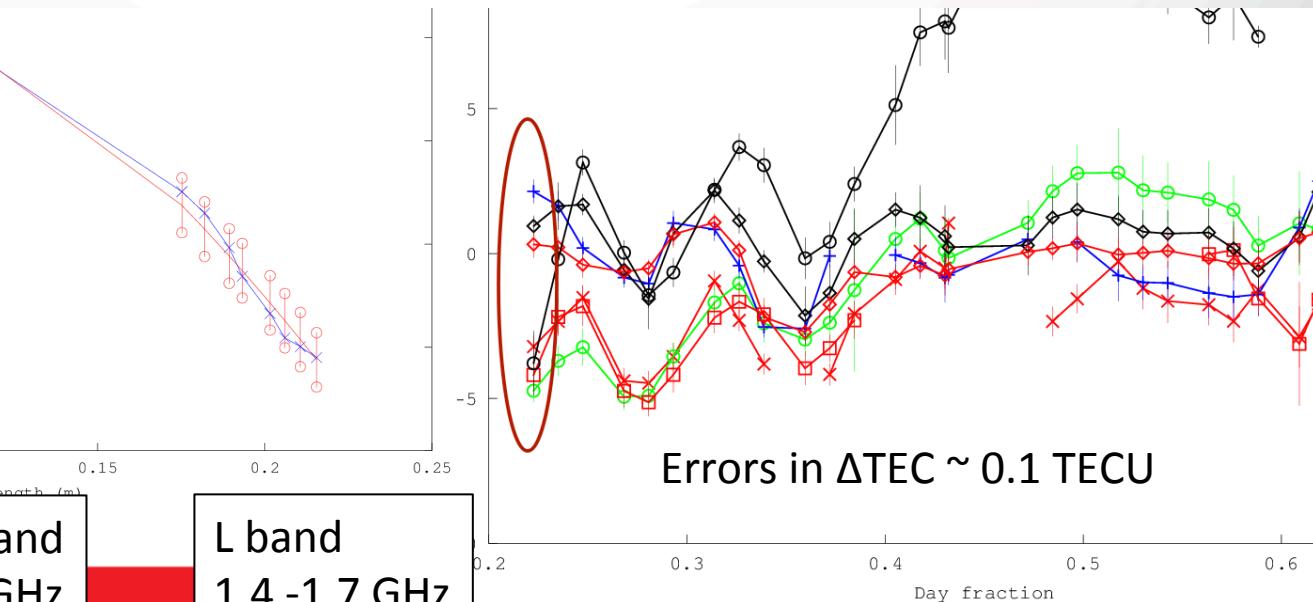
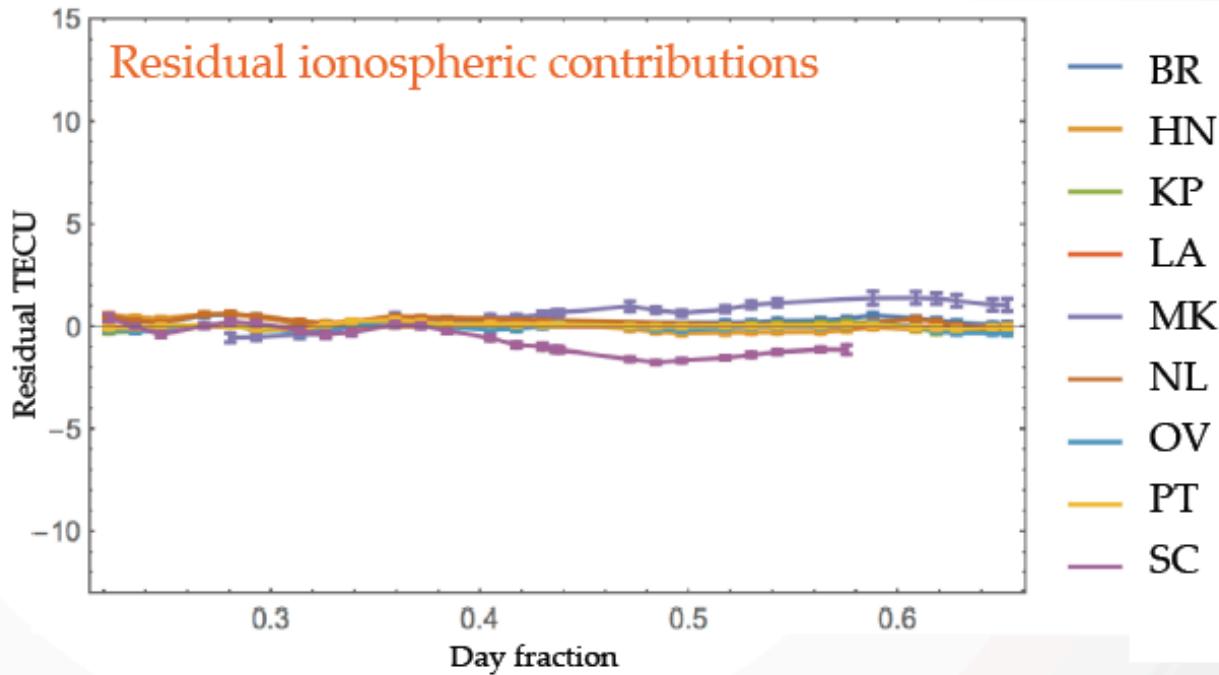
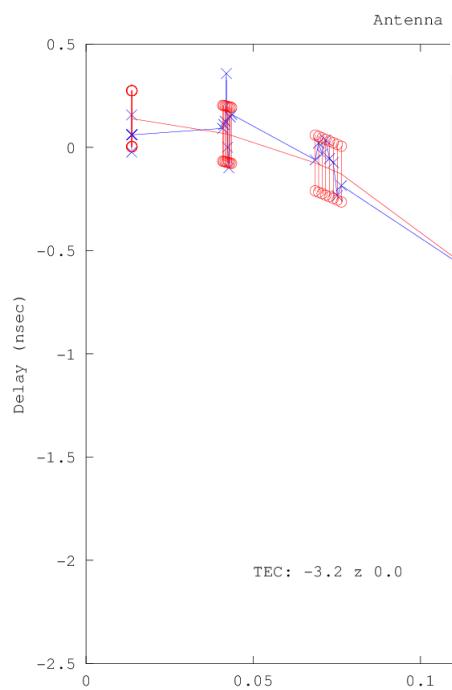
$$\text{TEC from } \tau = 1.34 \Delta \text{TEC} \nu^{-2} + \Delta \nu/c$$



Experiment

Solve for delay

TEC from



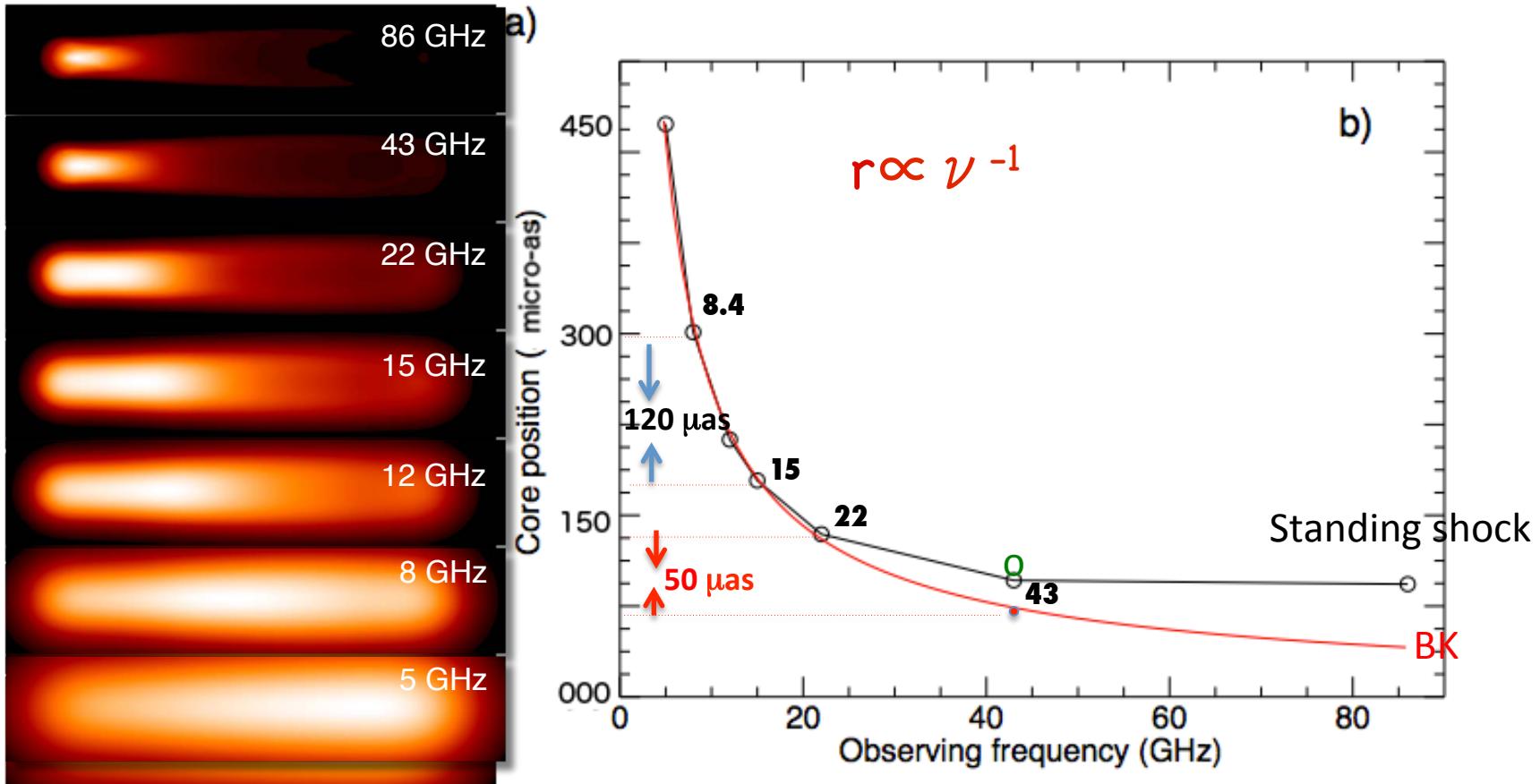
K band
21.8-22 GHz

Wide C band
3.9 - 7.9 GHz

L band
1.4 - 1.7 GHz

Preliminary Results on BL-Lac

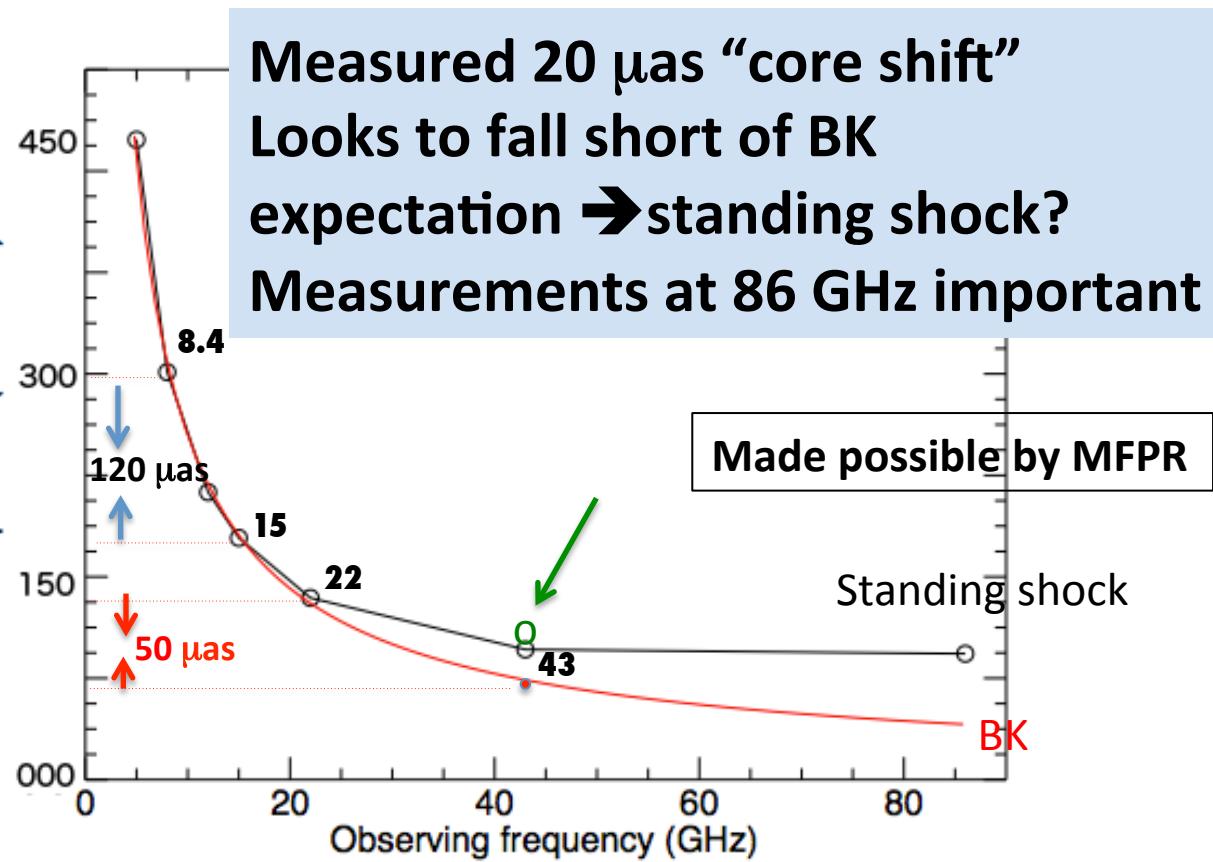
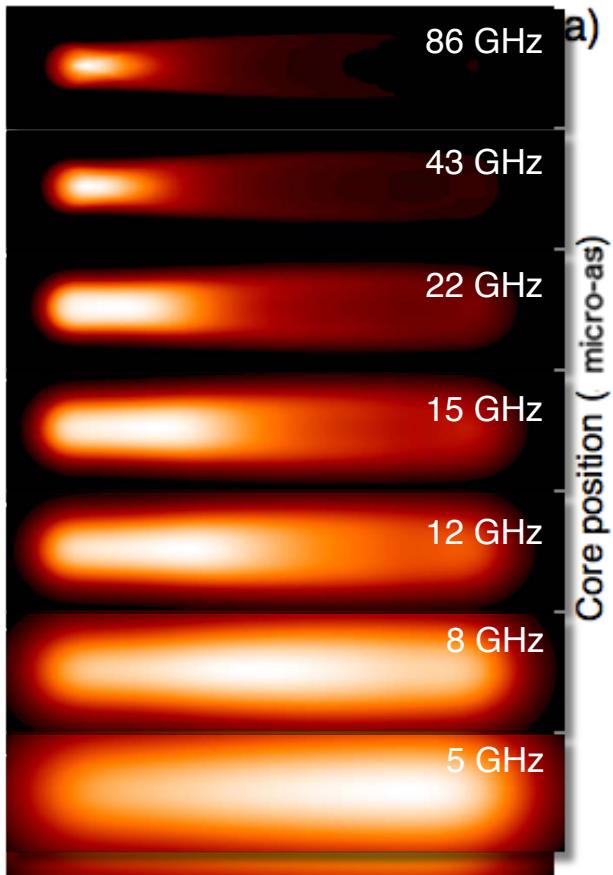
Use cm-results to provide scale. 8.4/15 GHz, 120 μ as



22/43 GHz *BK Predict* : $50 \pm 40 \mu$ as
 "core-shift"

Preliminary Results on BL-Lac

Use cm-results to provide scale. 8.4/15 GHz, 120 μ as



22/43 GHz
“core-shift”

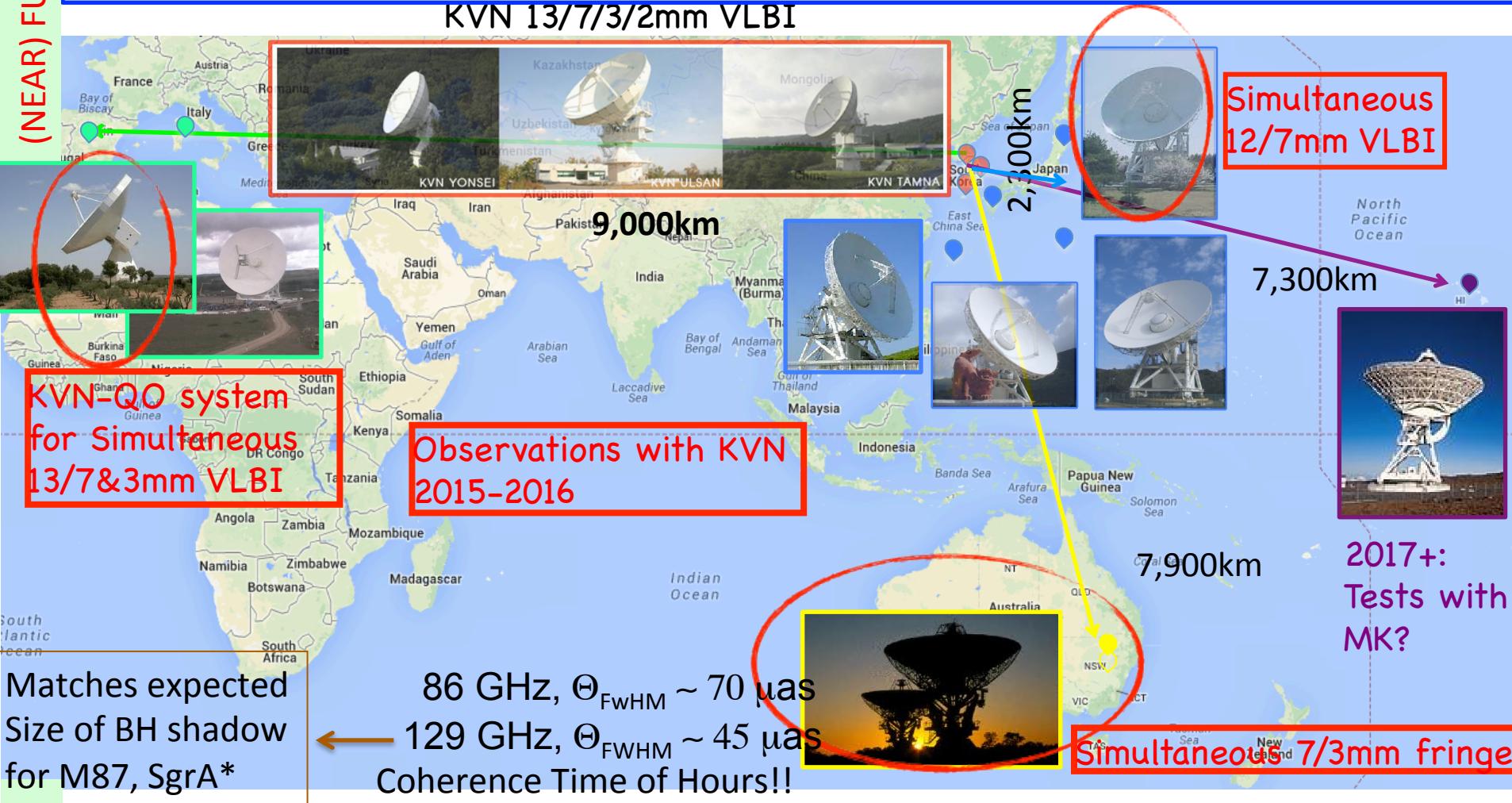
BK Predict : $50 \pm 40 \mu$ as

*Measured: $20 \pm 6 \mu$ as
with MFPR*

(NEAR) FUTURE

The quest for largEST angular resolution (=highEST astrometric accuracy): A Global “Multi-Frequency” mm-VLBI array

KVN 13/7/3mm VLBI



FUTURE

Techniques relevant for ALMA (long baselines)

(NEAR) FUTURE

The quest for largEST angular resolution (=highEST astrometric accuracy): A Global “Multi-Frequency” mm-VLBI array

KVN 13/7/3/2mm VLBI



Now:

VLBA with fast frequency switching (up to 86 GHz)

Future:

ngVLA (TBD)??? 1 - 100 GHz

Size of BH shadow
for M87, SgrA*

← 129 GHz, $\Theta_{FWHM} \sim 45 \mu\text{as}$
Coherence Time of Hours!!



Simultaneous 7/3mm fringes

FUTURE

Techniques relevant for ALMA (long baselines)



Summary

Potential of multi-frequency observations to improve the performance of mm-VLBI with new capabilities.

SFPR / MFPR enable:

- Superior tropospheric compensation, boost array with increased sensitivity.
- High precision “bona fide” astrometry at (sub-)mm-VLBI
- No upper frequency limit (B2B mode in ALMA at ca. 650 GHz)

Widely applicable, to many sources, enables new applications

Very effective use of observing time with simultaneous multi-freq. observations.

Technology ready, Slow telescope switching / Single source OK

Science made possible by SFPR /MFPR – widen applicability, beyond scope of PR:

SFPR: “Core-shift” VLBA “bona fide” astrometric measurements of M87 at 86-GHz

Spectral Index maps astrometrically aligned up to 130-GHz, for 5 sources

MFPR: “Core-shift” VLBA “bona fide” astrometric measurements of BL Lac at 43-GHz

Coherence time @ 132 GHz extended to 20 minutes (FPT) and > 8 hours (SFPR)



END